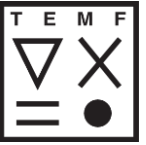


SINGLE MODE CAVITY FOR 3rd HARMONIC SYSTEM

Leon Kronshorst, Wolfgang Müller

DESY TEMF Collaboration Talks



CONTENT

1 Introduction to 3rd Harmonic Systems

2 Cavity Design

3 Regional Sensitivity Analysis

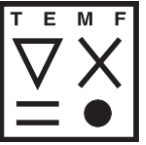
4 Optimization

5 Higher Order Modes Investigation

6 Wake Impedances

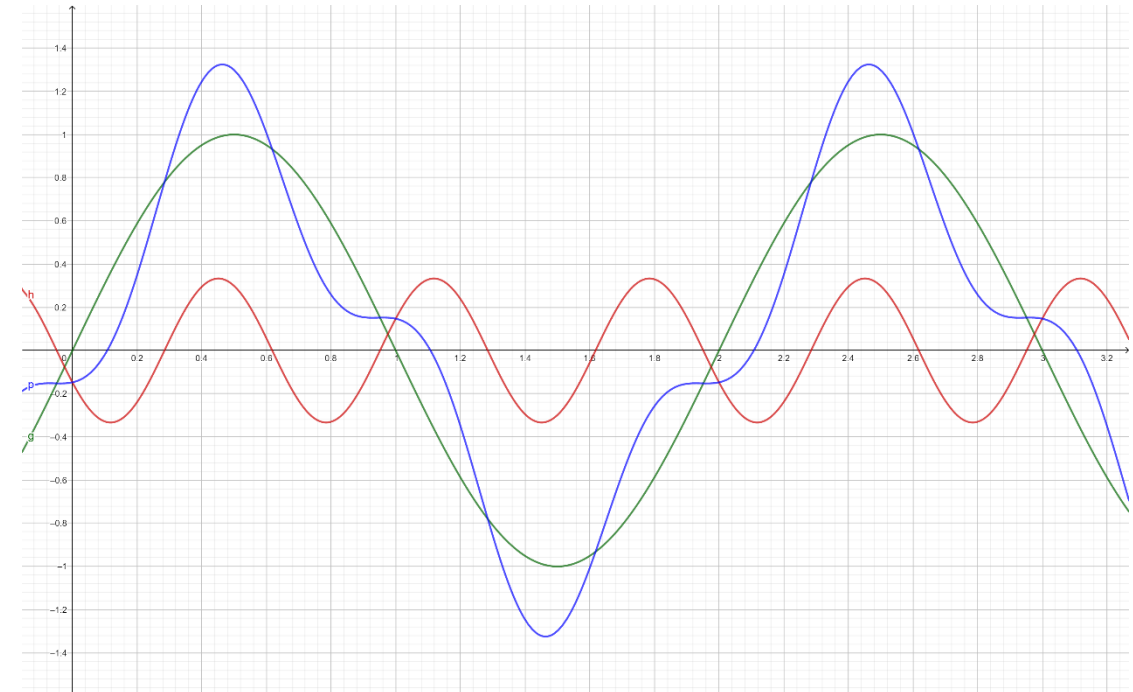
7 Addition of Nosecones

8 Outlook



INTRODUCTION TO 3rd HARMONIC SYSTEMS

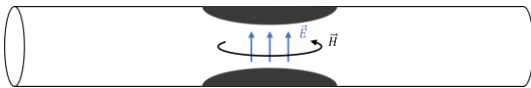
- Goal: Bunch lengthening
 - Achieves reduction of:
 - Touchek Effect
 - Intrabeam scattering
 - Longer Beam Lifetime
 - Lower Emittance



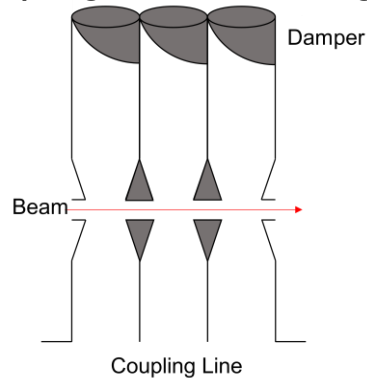
CAVITY DESIGN PROGRESS

- Starting Point: Design ideas from Herminghaus

- Circular cylindrical waveguide with indentations



- Stacking multiple cells together and damping in the Waveguide

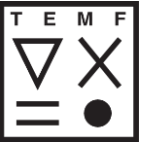


- Approx. figures of merit

Q_0	15000
R_s	44.58 MΩ

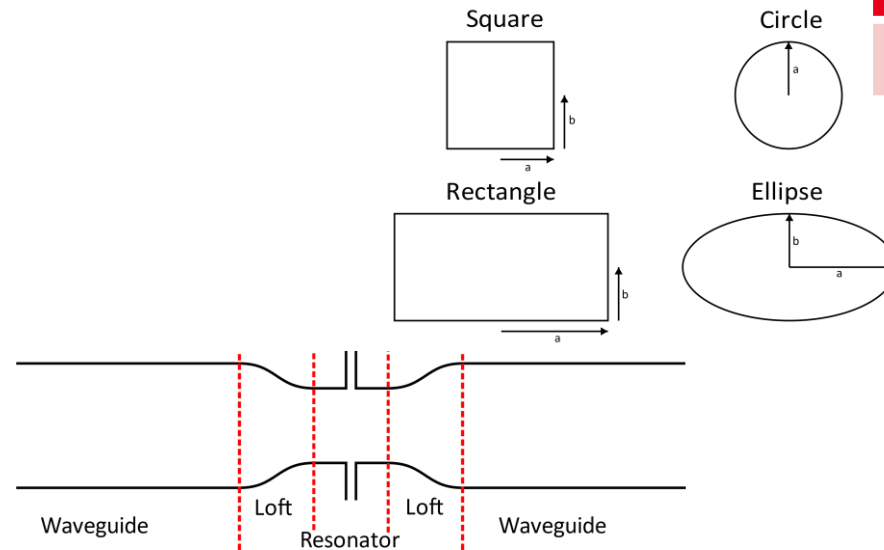


CAVITY DESIGN PROGRESS



- Next step: Geometry investigation

- Combining different crosssections for waveguide and resonator section

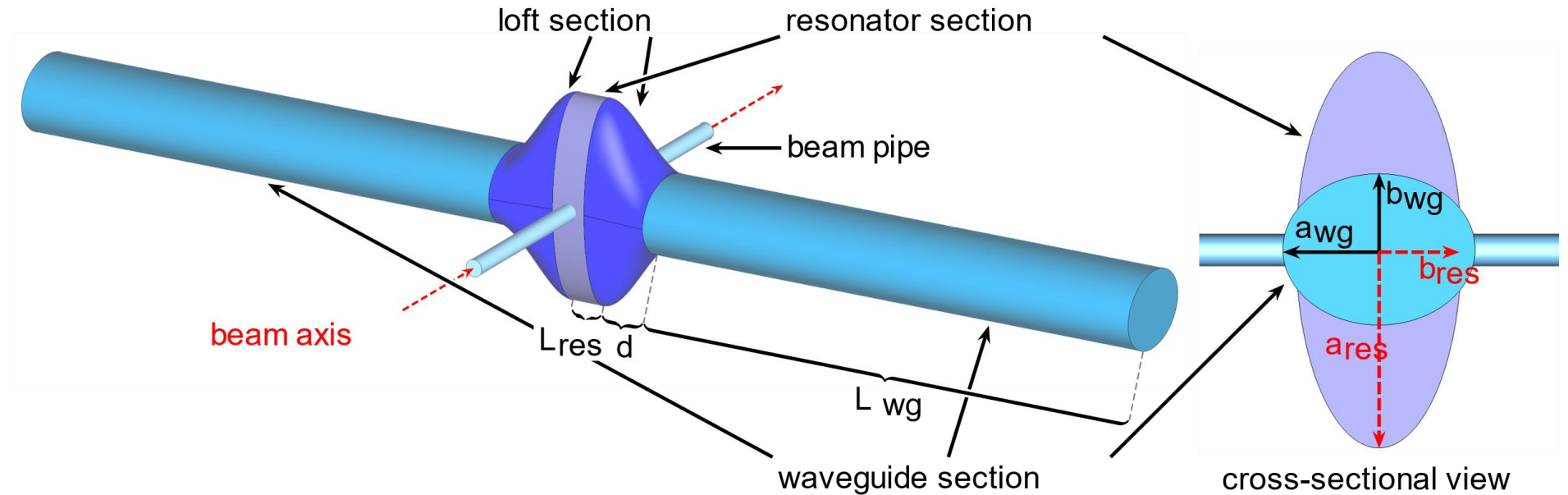


- Approx. figures of merit

Q_0	16000
R_s	1.82 M Ω

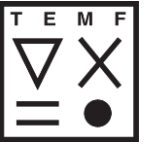
CAVITY DESIGN

CURRENT STATE



Reasoning

- Strong decoupling between waveguide and resonator
- No sharp edges

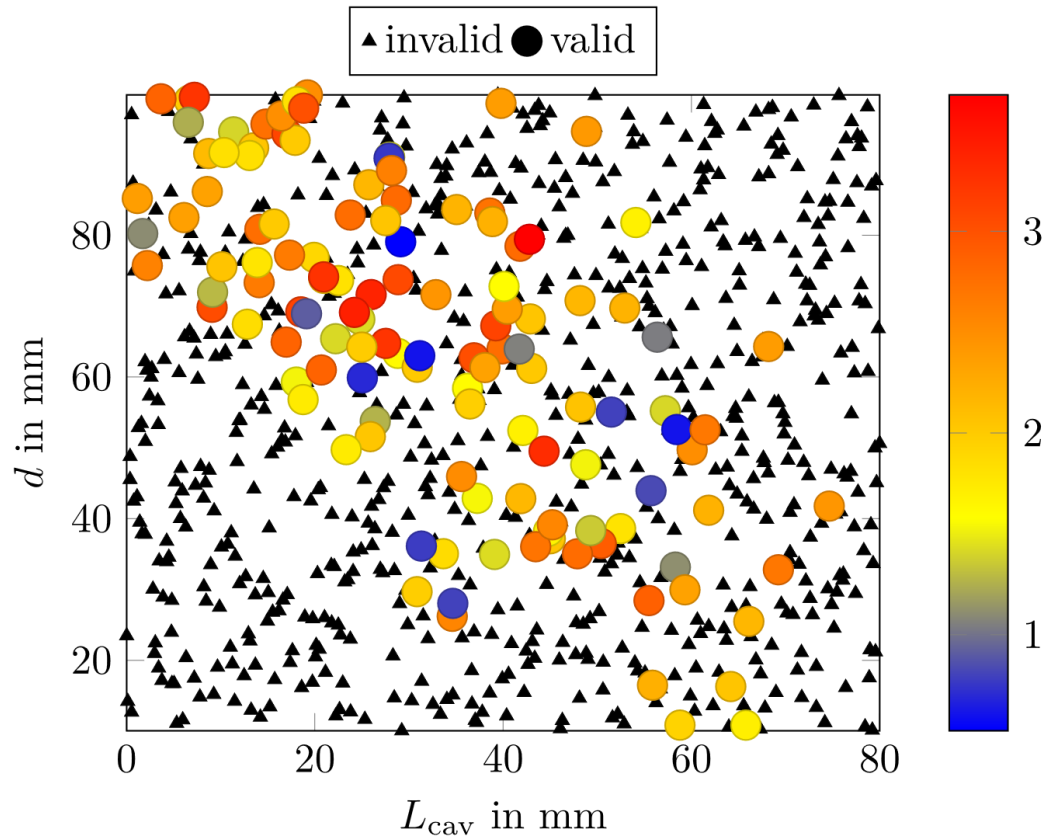


REGIONAL SENSITIVITY ANALYSIS

- Many valid parameter combinations
 - Difficult task for common optimizer
 - How to obtain needed knowledge?
- Sensitivity Analysis (SA)
 - Estimating influences of individual parameters on the model result through sampling
 - Understand the influence of parameter combinations
- Regional Sensitivity Analysis (RSA)
 - Type of SA
 - Only 100 - 1000 x M samples necessary
 - M – number of parameters
 - Map the input space to different regions of interest
 - Typically, desired $y \in Y_b$ and not desired $y \in Y_{nb}$
- Allows for targeted optimization and parameter space reduction

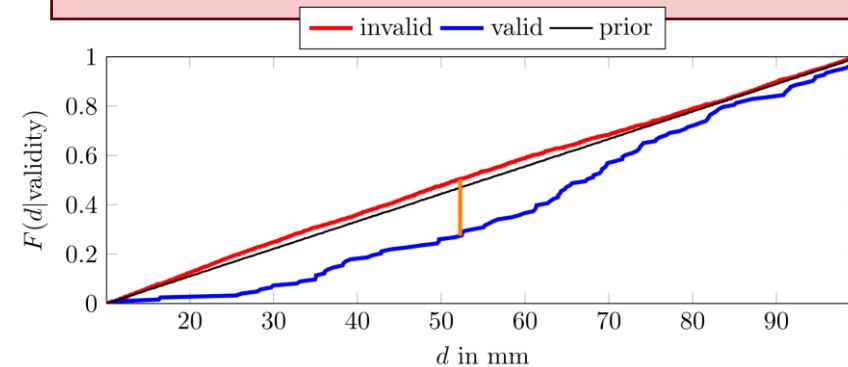
REGIONAL SENSITIVITY ANALYSIS

1. Visual RSA

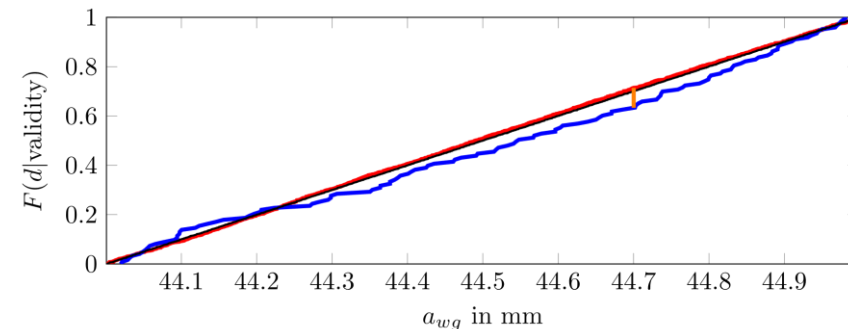


2. Statistical RSA using Kolmogorov-Smirnov statistic

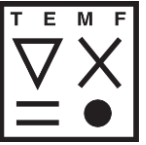
$$S_i = \max_{x_i} |F(x_i|y_b)(x_i|y \in Y_b) - F(x_i|y_{nb})(x_i|y \in Y_{nb})|$$



$$S_d = 0.2304$$

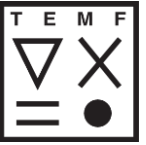


$$S_{a_{wg}} = 0.0808$$



CAVITY OPTIMIZATION REQUIREMENTS & GOALS

- Resonant frequency $f_1 = 1.5$ GHz
 - it being a qTE111,even-mode
 - Waveguide cutoff-frequency $f_c \approx 2$ GHz
 - 2nd Eigenmode resonant frequency $f_2 > f_c$
- Mitigate all relevant Higher Order Modes
 - Maximize:
 - Q_0 - unloaded Quality Factor
 - R_s - Shuntimpedance
 - λ_{TTF} - Transit Time Factor
 - ε - Efficiency

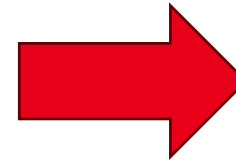


CAVITY OPTIMIZATION EFFICIENCY

- Proposed figure of merit:

$$\text{Efficiency } \varepsilon := \frac{\Delta U}{P_e}$$

- ΔU - is the energy gain of the particle per cavity passage
- P_e - is the required externally supplied power



$$\varepsilon \propto \frac{V_{acc}}{P_{\text{cavity loss}}}$$

- With:

$$\bullet \Delta U = -Q V_{acc} = Q \int_{-\frac{L}{2}}^{\frac{L}{2}} \vec{E} e^{-j\omega \frac{z}{\beta c}} \cdot d\vec{z}$$

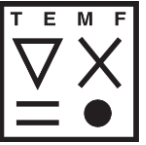
$$\bullet P_e = P_{\text{couple loss}} + P_{\text{cavity loss}} + P_{\Delta U}$$

- And

$$\bullet P_{\text{couple loss}} + P_{\Delta U} \ll P_{\text{cavity loss}}$$

Possibly better choice than individually optimizing for:

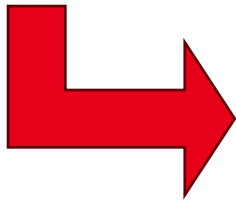
$$R_s, Q, \frac{R_s}{Q} \text{ or } \lambda_{\text{TTR}}$$



CAVITY OPTIMIZATION PROCESS

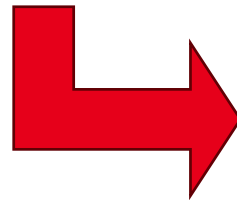
1. Performing RSA

- Enabling the adjustment of parameter ranges
- Provide a starting point for further optimization
 - i.e. a parameter set with a high efficiency ε



2. Optimizing for f_1

- Reaching target of 1.5 GHz
- Maintaining $f_2 > f_c$ and a high ε

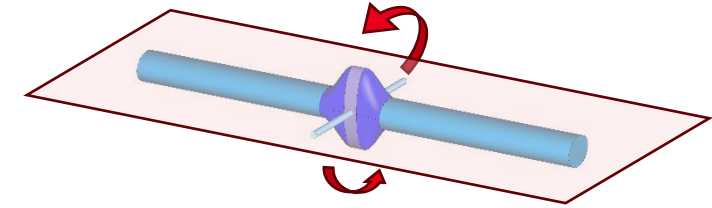
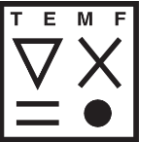


3. Optimizing for ε

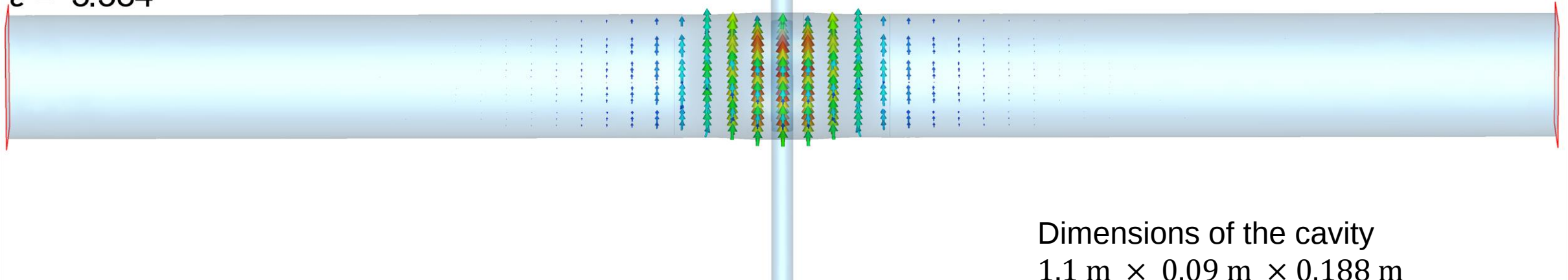
- Final increment in ε
- Maintaining $f_1 = 1.5$ GHz and $f_2 > f_c$



CAVITY OPTIMIZATION RESULTS



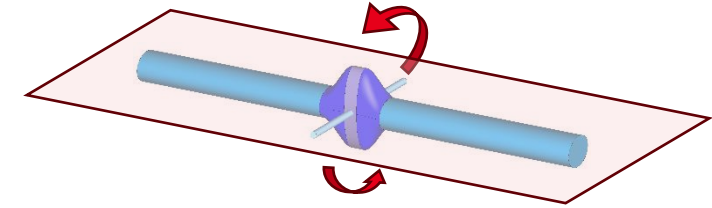
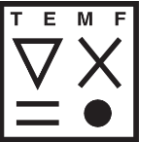
Ground Mode-qTE₁₁₁,even
 $f_1 = 1.5005 \text{ GHz}$
 $Q_0 = 23247.3$
 $\epsilon = 3.384$



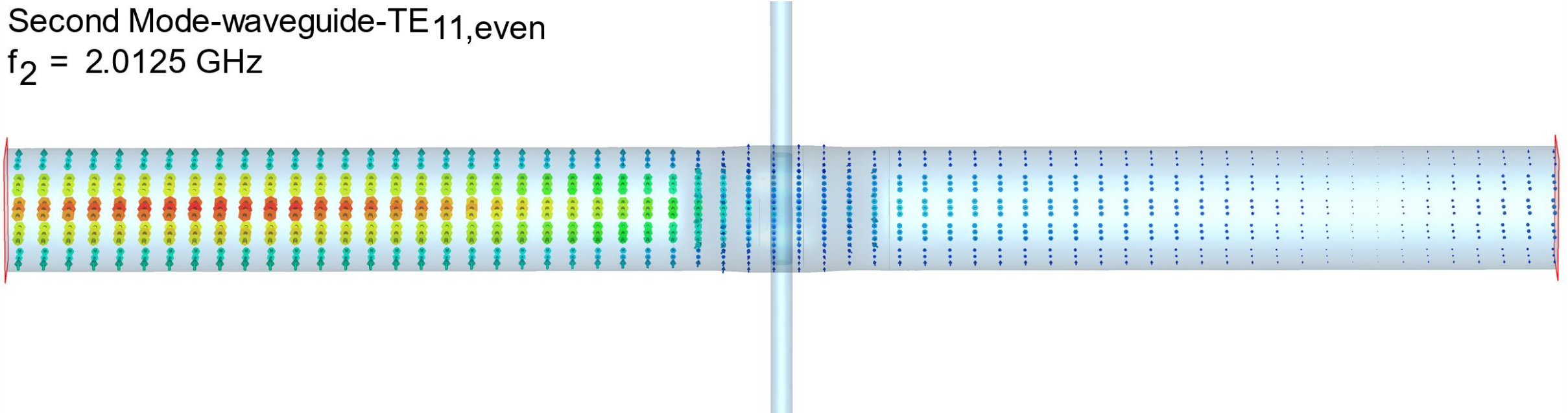
Dimensions of the cavity
 $1.1 \text{ m} \times 0.09 \text{ m} \times 0.188 \text{ m}$



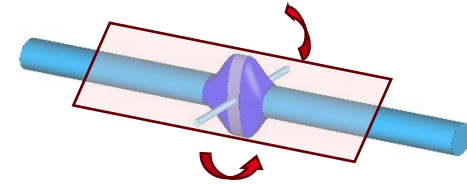
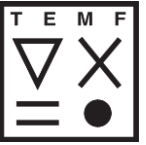
CAVITY OPTIMIZATION RESULTS



Second Mode-waveguide-TE₁₁,even
 $f_2 = 2.0125$ GHz



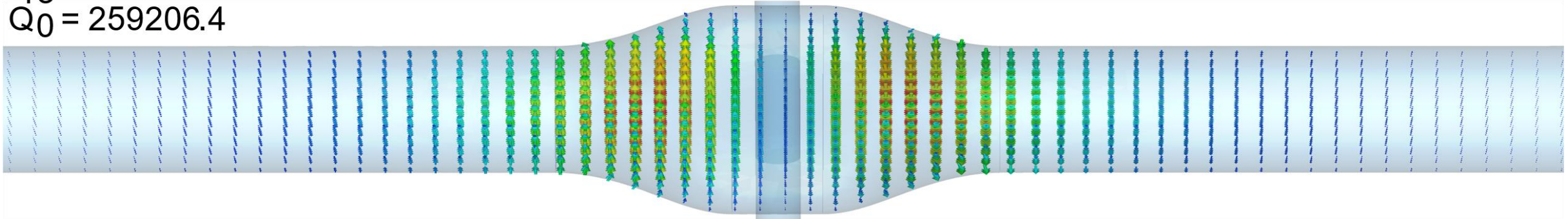
HIGHER ORDER MODES INVESTIGATION

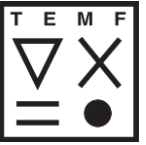


qTE_{112,even}

$f_{13} = 2.2499 \text{ GHz}$

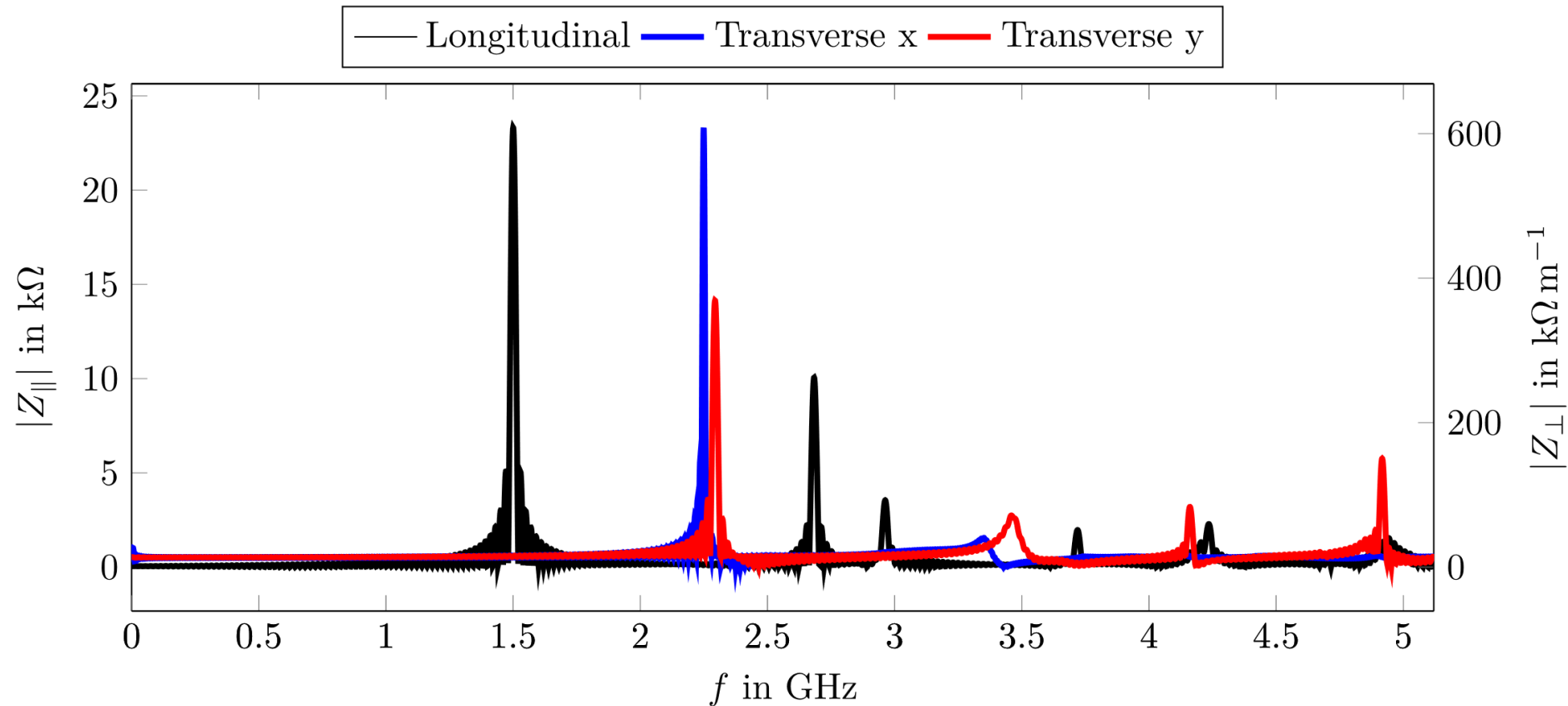
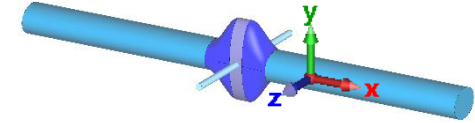
$Q_0 = 259206.4$

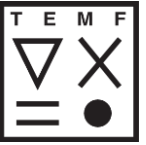




HIGHER ORDER MODES INVESTIGATION

Wake Impedances

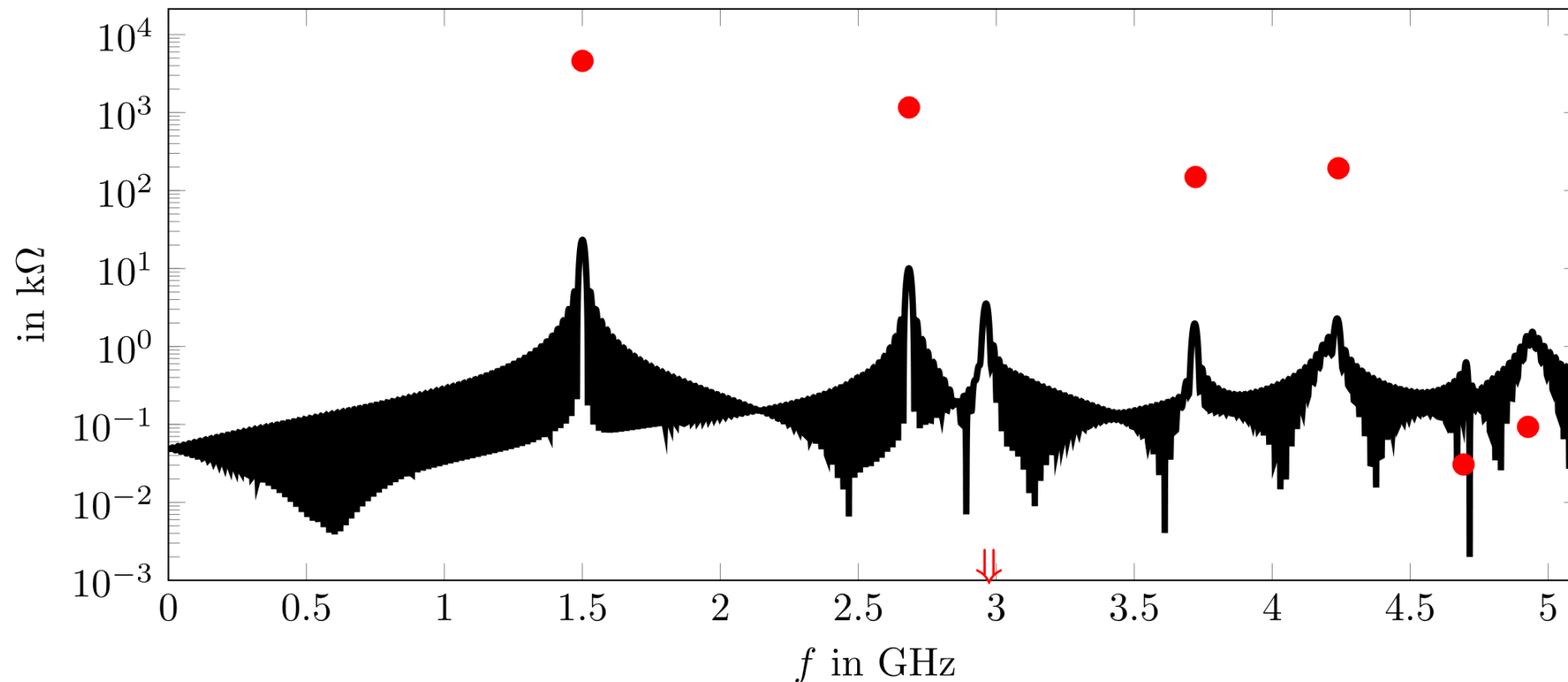




WAKE IMPEDANCES

LONGITUDINAL

— Longitudinal Wake Impedance ● Eigenmode Shunt Impedance

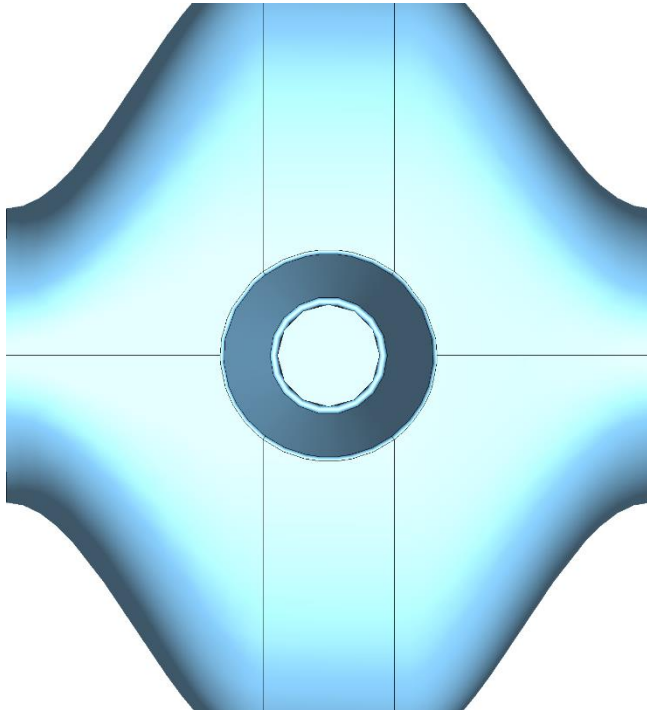


$$Z_{\parallel}(\omega) = \frac{R_S}{1 + jQ_r(\omega/\omega_r - \omega_r/\omega)}$$

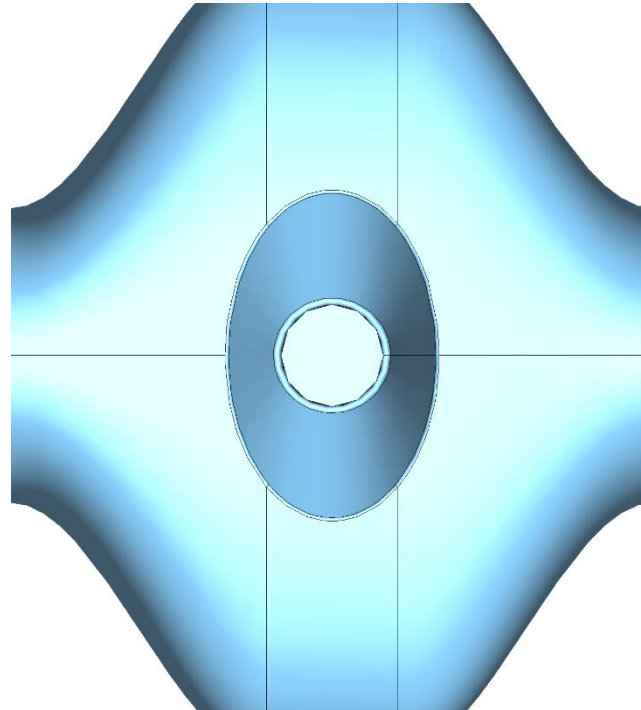
$$\Rightarrow Z_{\parallel}(\omega_r) = R_S$$

ADDITION OF NOSECONES

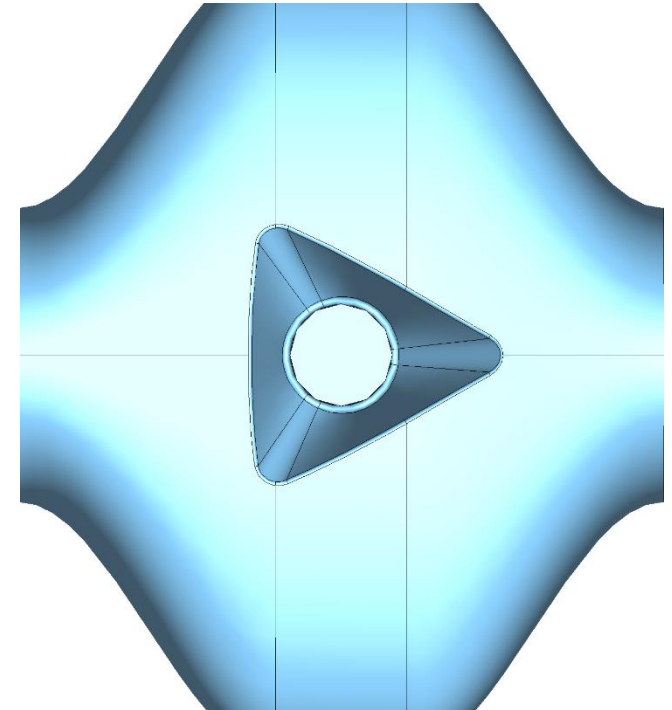
1. Regular Nosecone



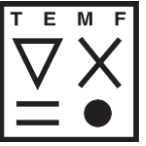
2. Elliptical Nosecone



3. Triangular Nosecone



None of the designs led to the desired reduction



OUTLOOK

- Promising results for ground mode and general functioning of cavity
- HOM's need further investigation
 1. Convergence study of the wake impedance using the wakefield solver
 2. Calculating the transverse shunt impedance from eigenmode results
 3. Changing the 2 waveguides to lead to asymmetries in resonator section
 4. Adding 2 more waveguides
- Additional possible work
 - Investigating the efficiency ε of known and build cavities
 - Further sensitivity analysis using variance-based methods
 - Comparing the optimization ansatz to popular methods