

Numerical Analysis of Wave Propagation in a Tapped Hole used as a Slow Wave Structure



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Wolfgang Ackermann, Herbert De Gersem

Institute for Accelerator Science and Electromagnetic Fields (TEMF), TU Darmstadt

DESY-TEMF-CANDLE
Summer Meeting on Video
21st September 2021

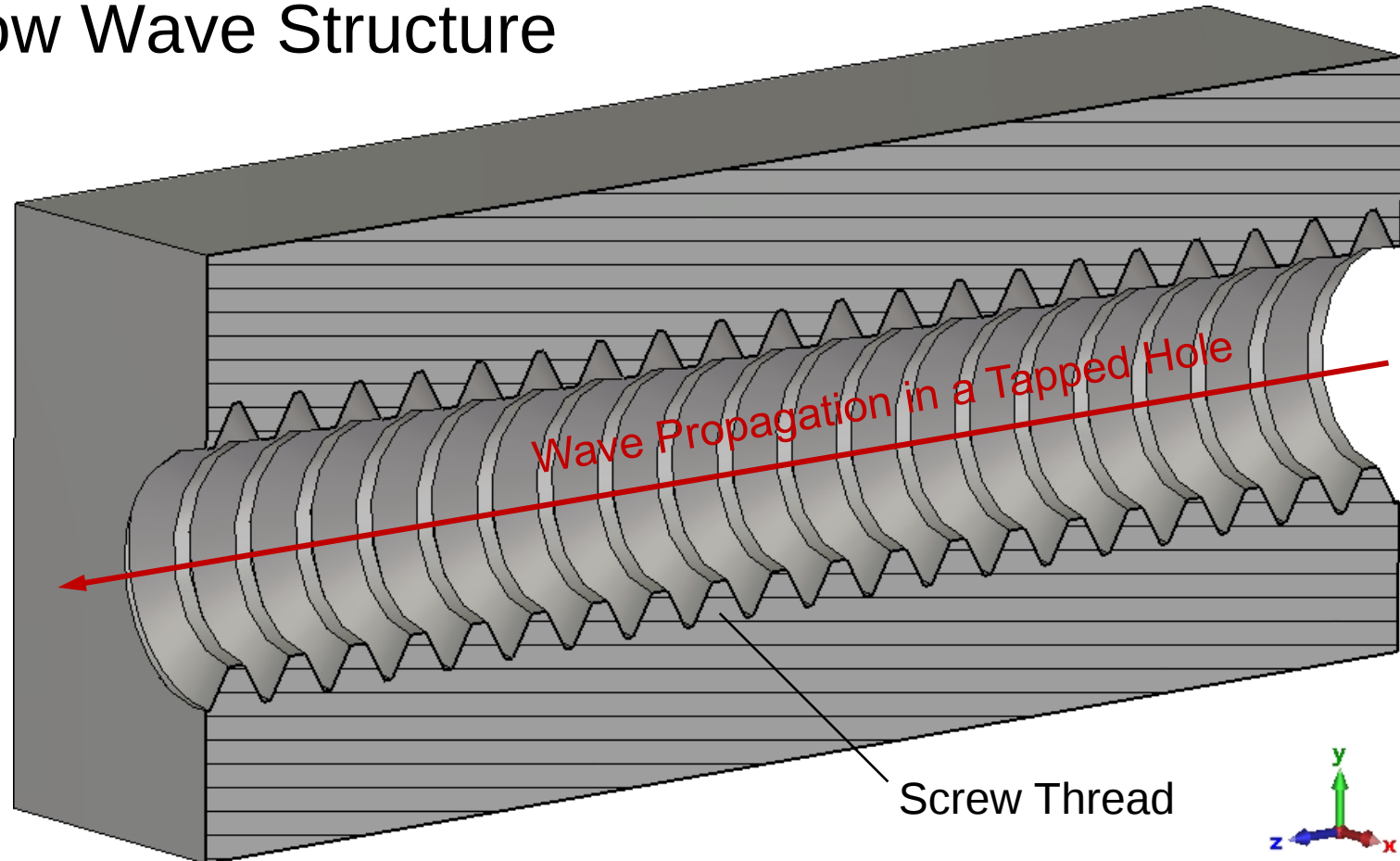


- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

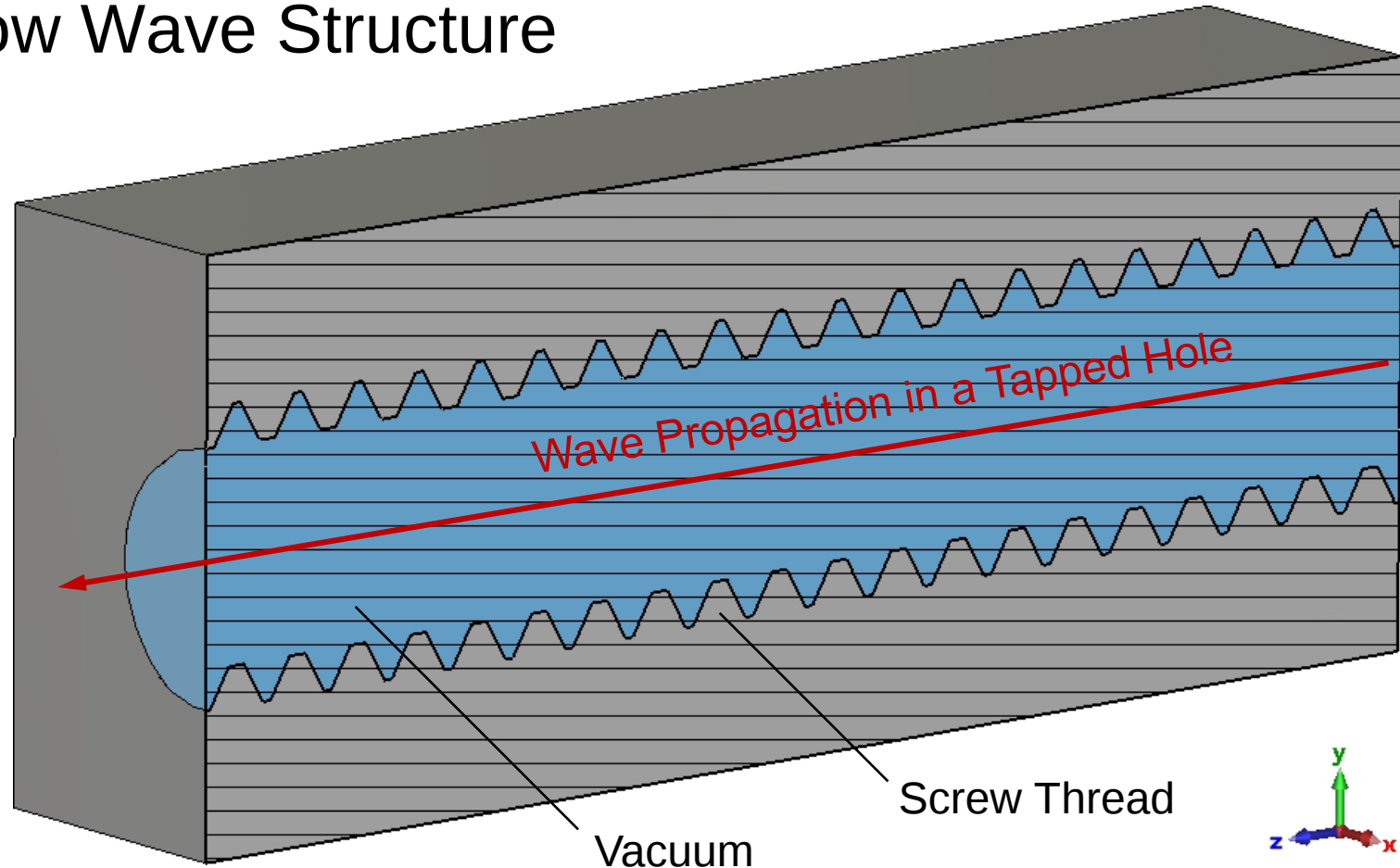
Motivation

- Slow Wave Structure



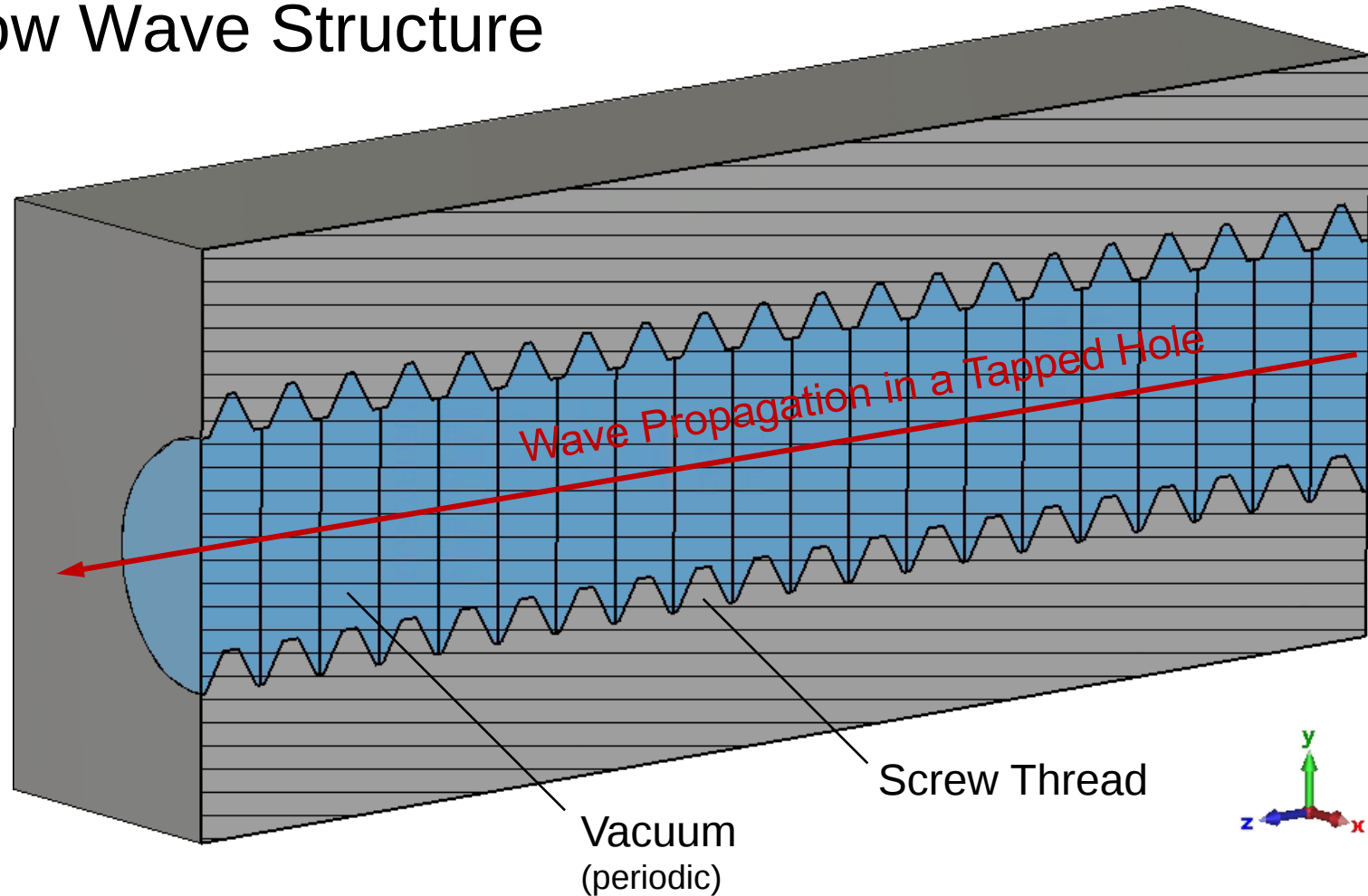
Motivation

- Slow Wave Structure



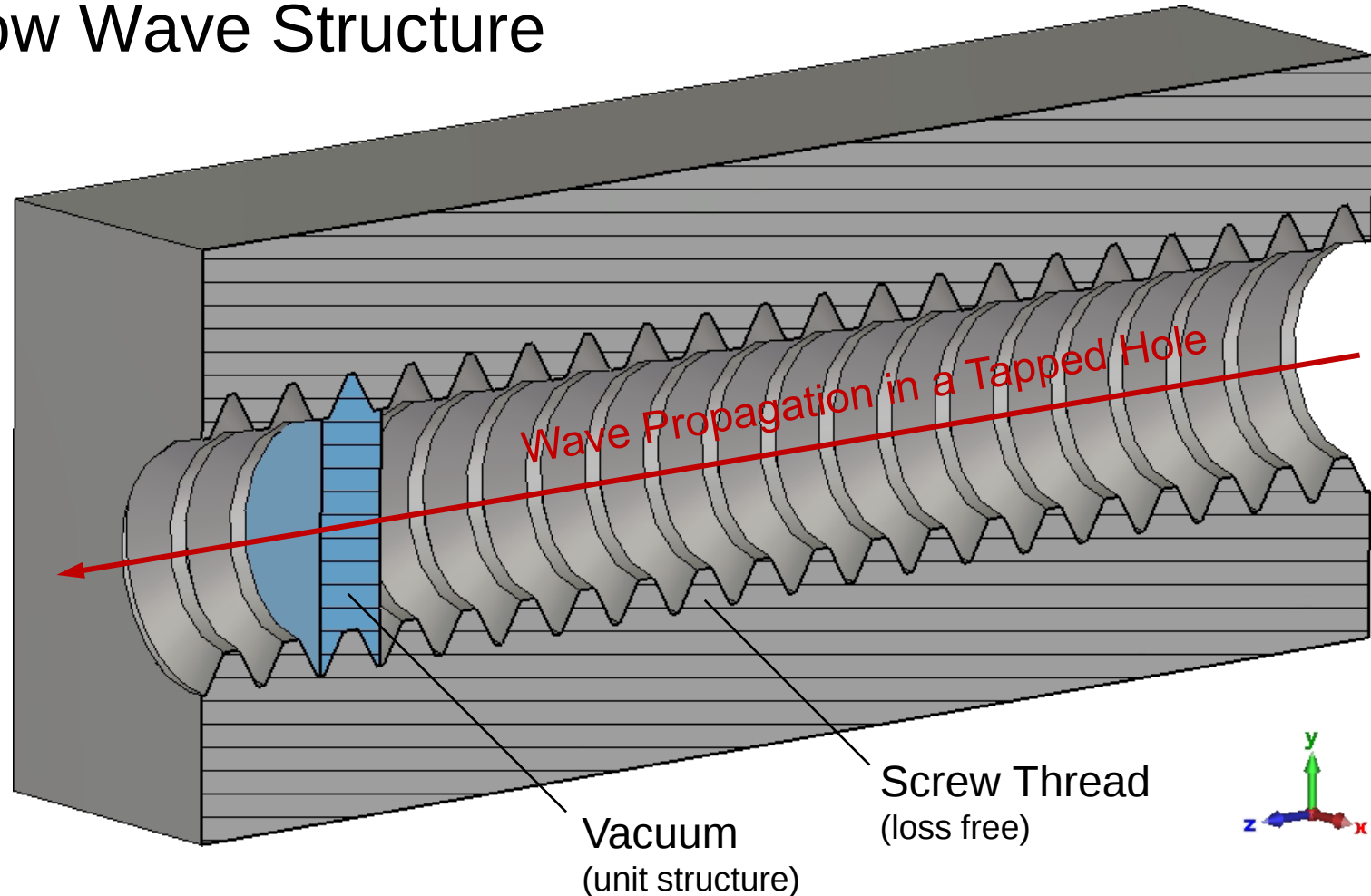
Motivation

- Slow Wave Structure



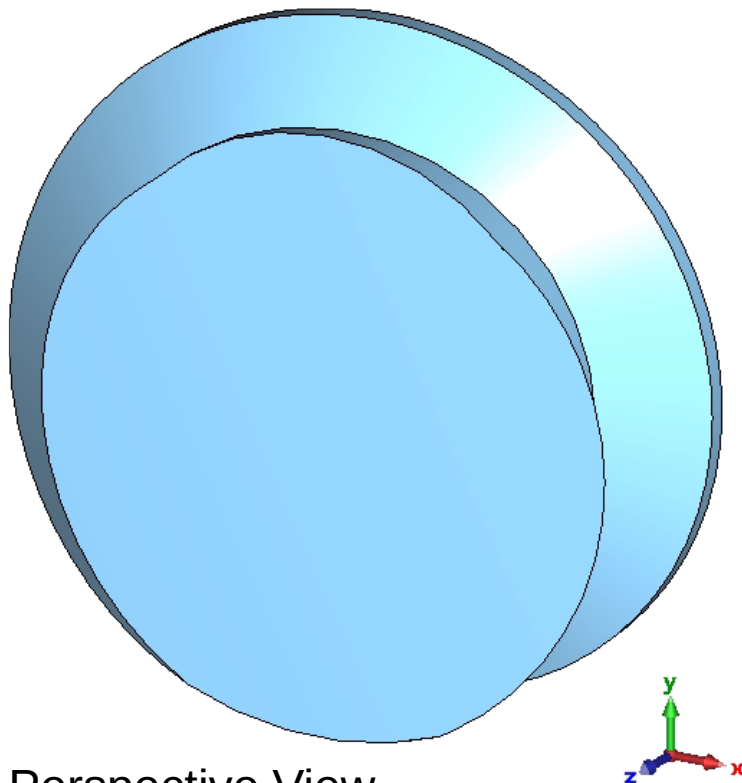
Motivation

- Slow Wave Structure



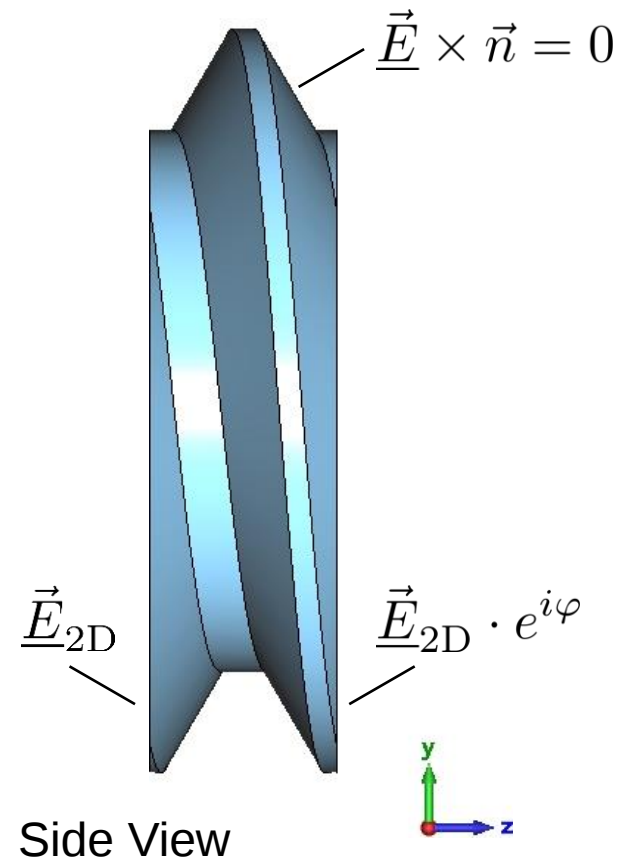
- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

▪ Slow Wave Unit Structure



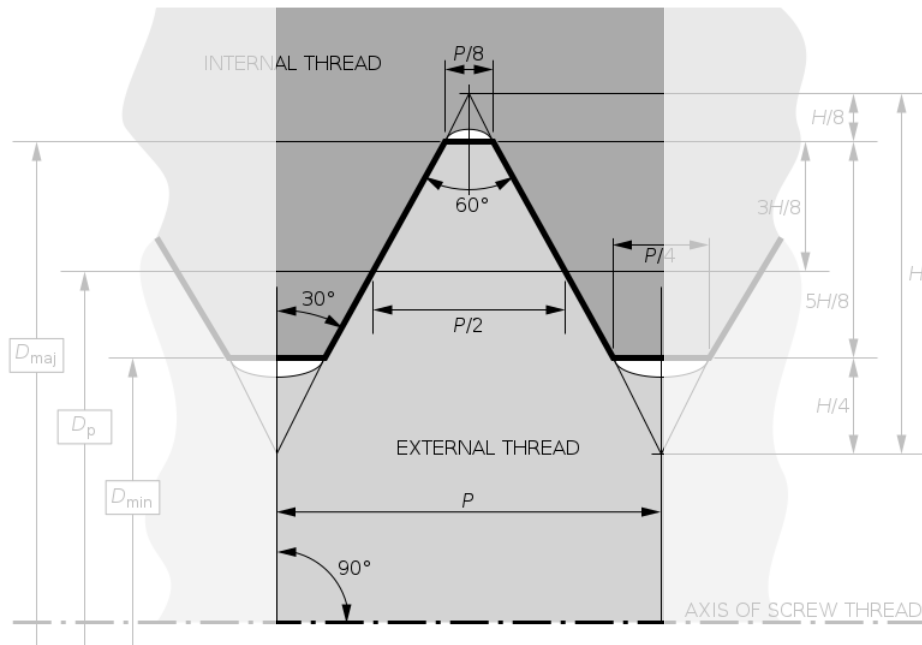
Perspective View

$$\text{curl} \frac{1}{\mu} \text{curl} \vec{E} = \omega^2 \varepsilon \vec{E}$$



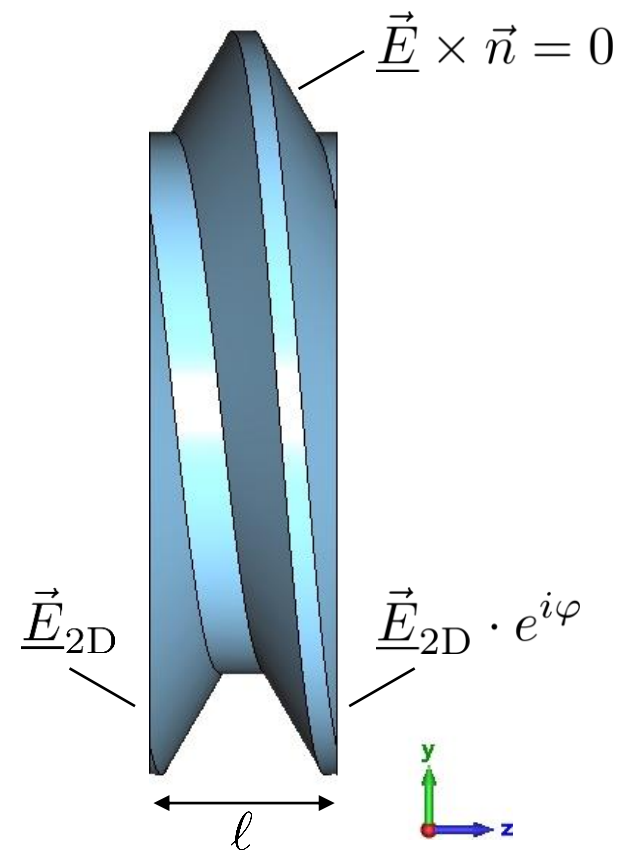
Side View

▪ Slow Wave Unit Structure

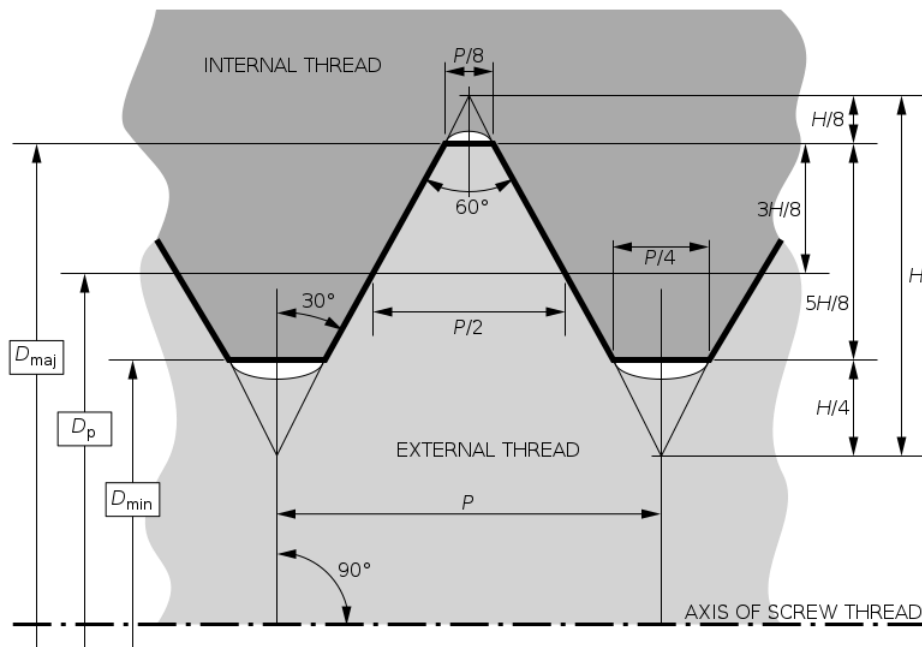


https://en.wikipedia.org/wiki/ISO_metric_screw_thread

$$\text{curl} \frac{1}{\mu} \text{curl} \vec{E} = \omega^2 \varepsilon \vec{E}$$



▪ Slow Wave Unit Structure (ISO metric screw thread)

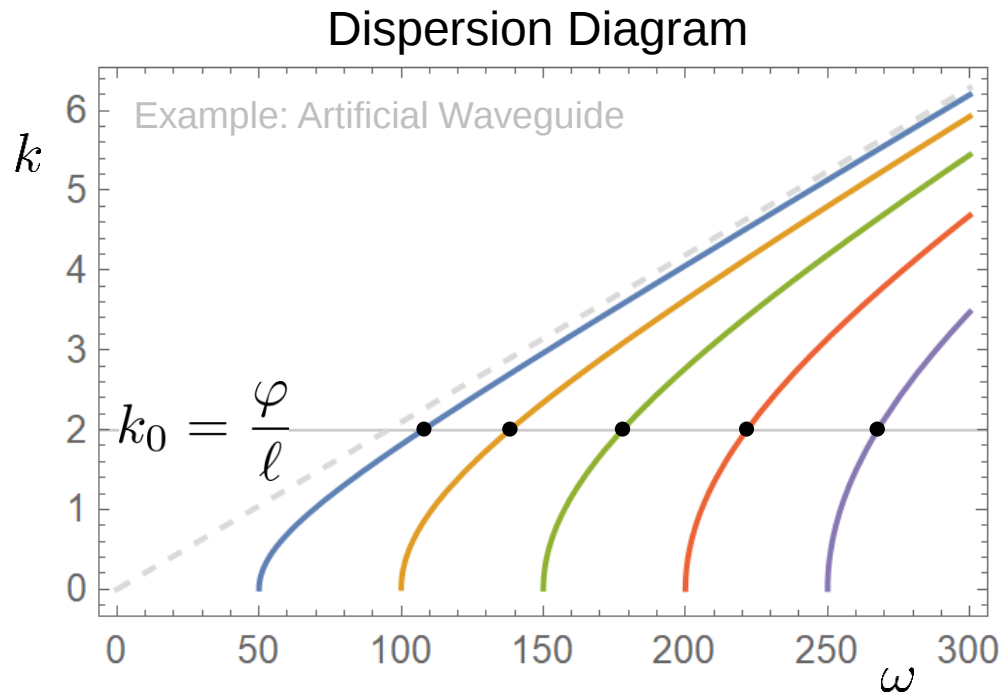


	D_{maj}	D_{min}	p
M1.0	1.0	0.729	0.25
M1.2	1.2	0.929	0.25
M1.4	1.4	1.075	0.30
M1.6	1.6	1.221	0.35
M1.8	1.8	1.421	0.35
M2.0	2.0	1.567	0.40

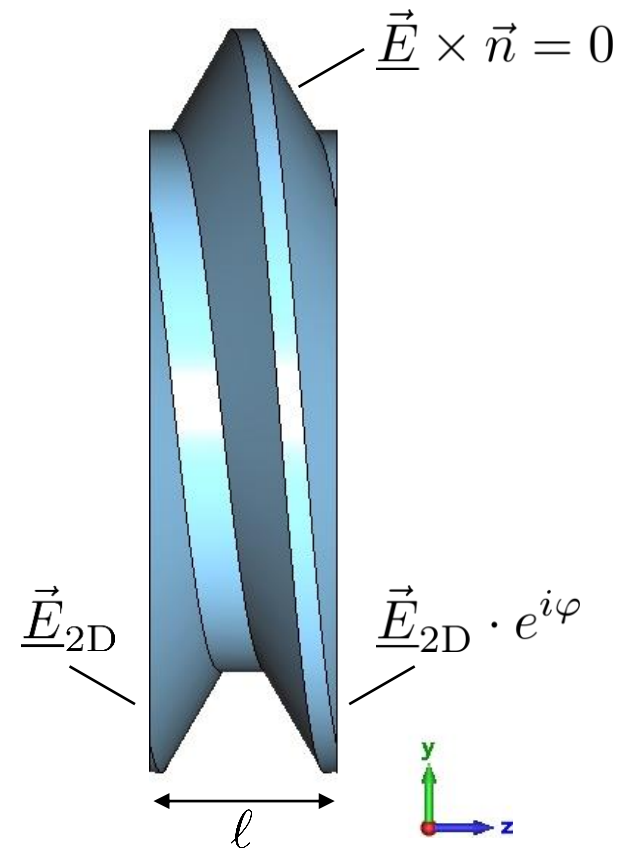
unit of measure: mm

https://en.wikipedia.org/wiki/ISO_metric_screw_thread

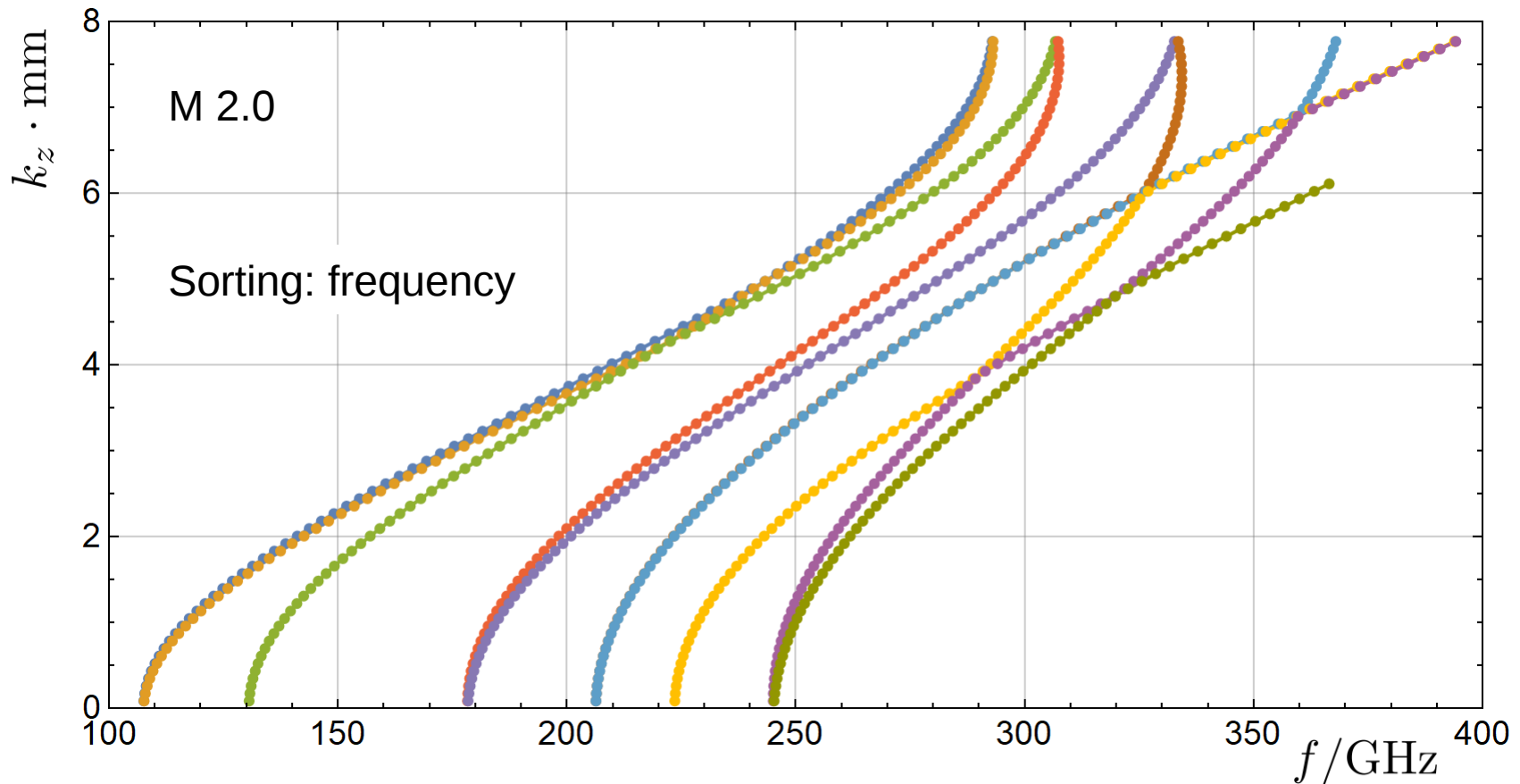
▪ Slow Wave Unit Structure



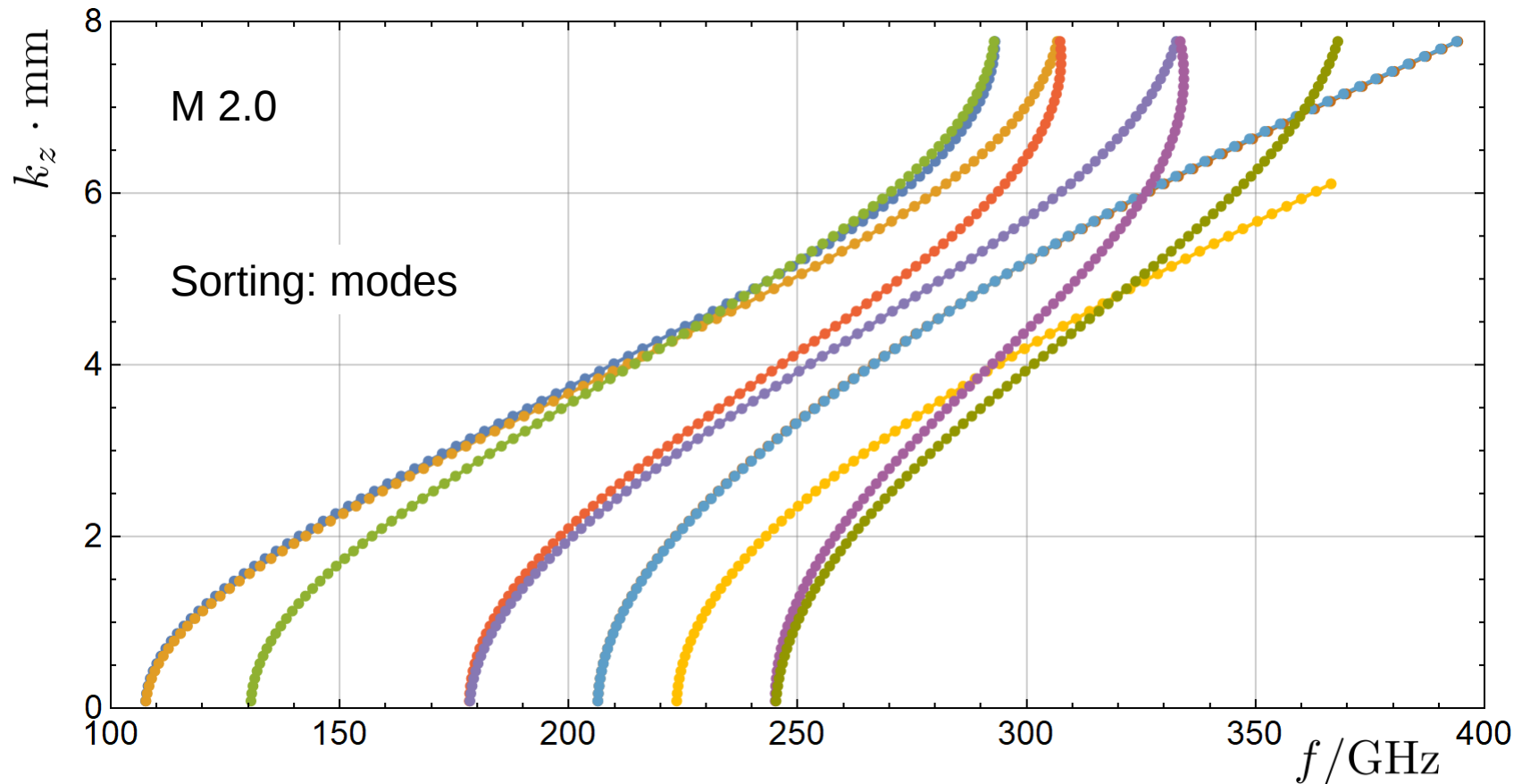
$$\text{curl} \frac{1}{\mu} \text{curl} \vec{E} = \omega^2 \varepsilon \vec{E}$$



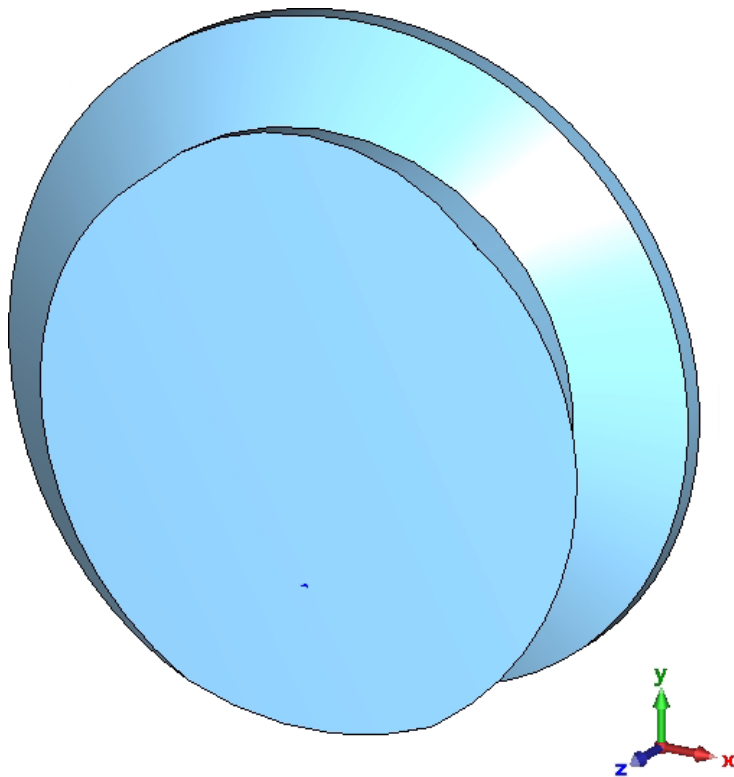
■ Dispersion Diagram (ISO metric screw thread)



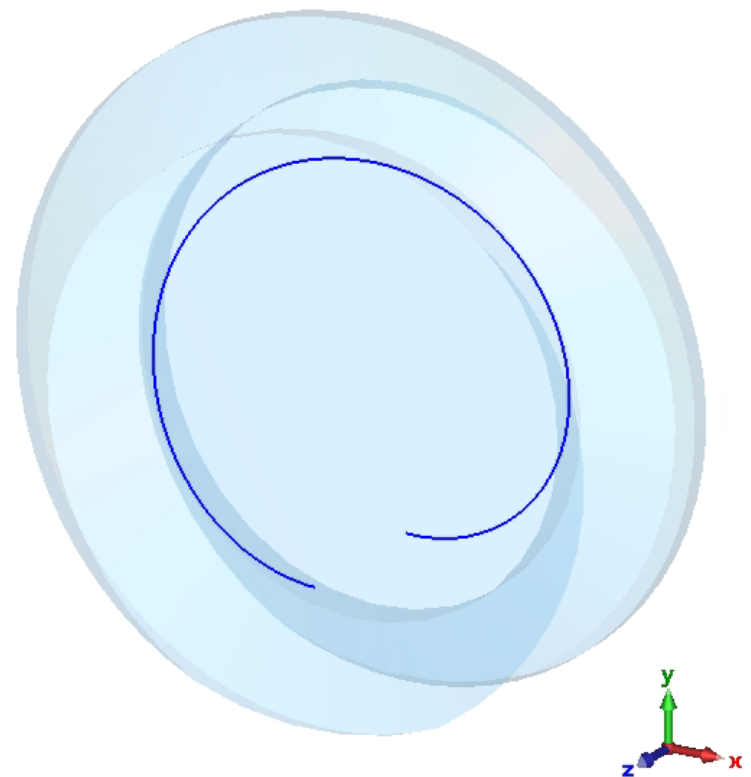
■ Dispersion Diagram (ISO metric screw thread)



- Slow Wave Unit Structure



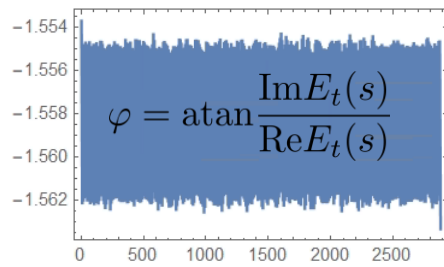
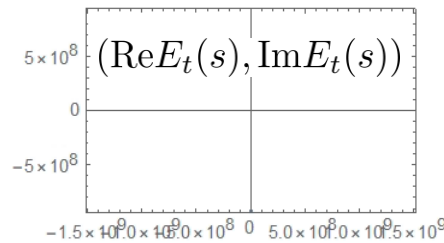
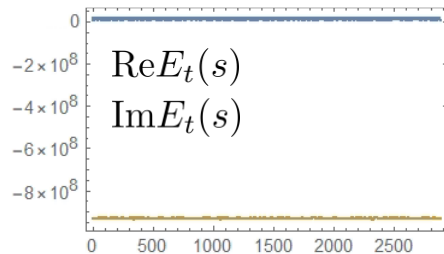
Perspective View



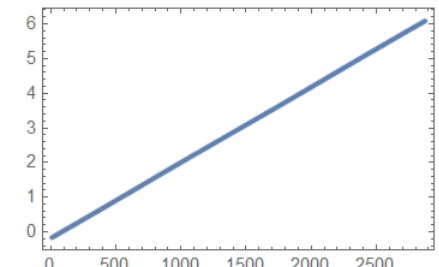
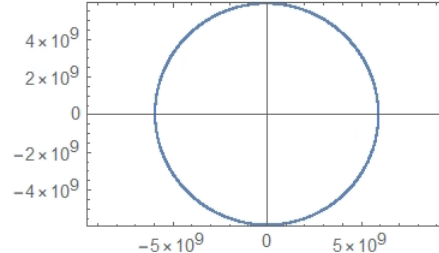
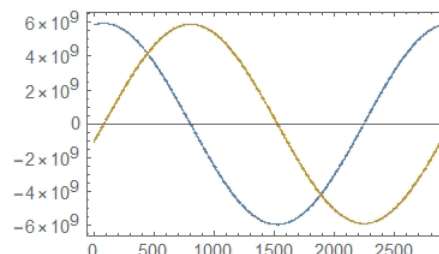
Field Evaluation Path (Helix)

■ Determination of the Azimuthal Order

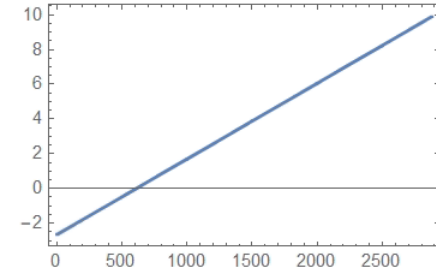
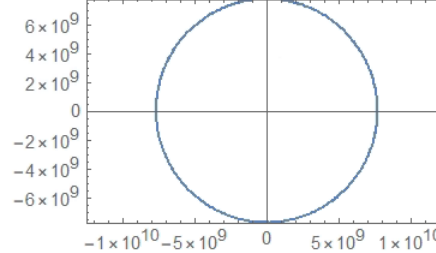
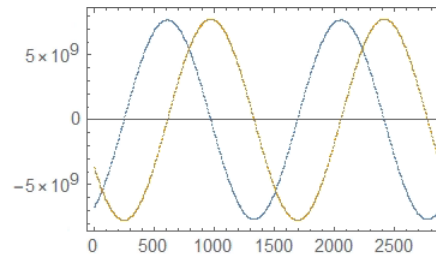
$$n_\varphi = 0$$



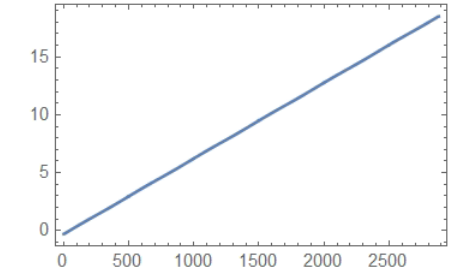
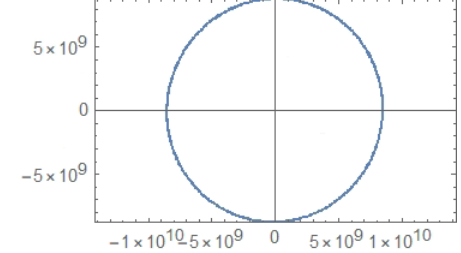
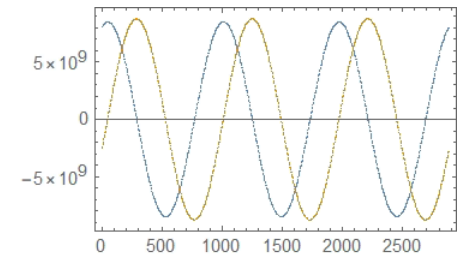
$$n_\varphi = 1$$



$$n_\varphi = 2$$



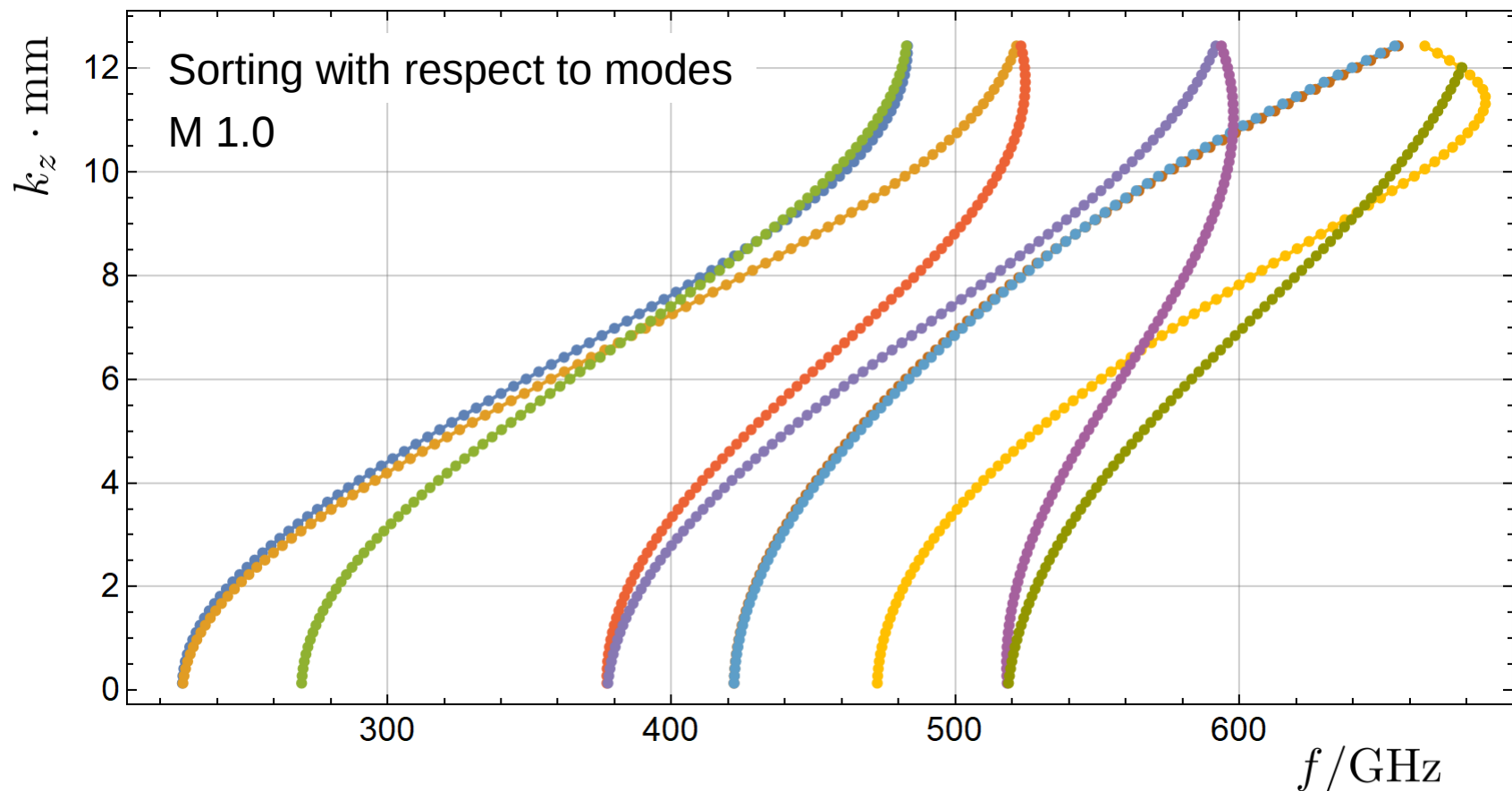
$$n_\varphi = 3$$



- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

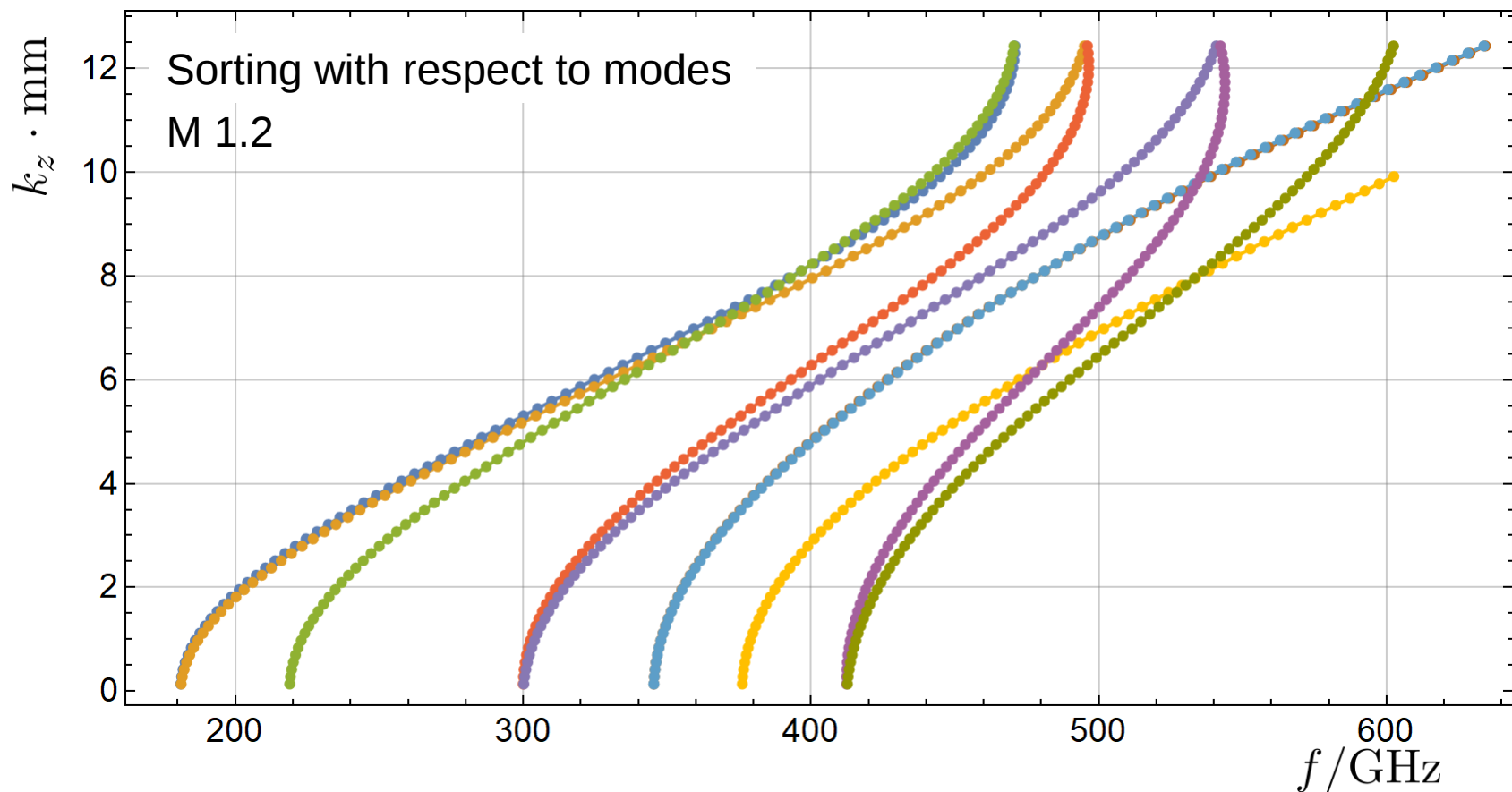
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



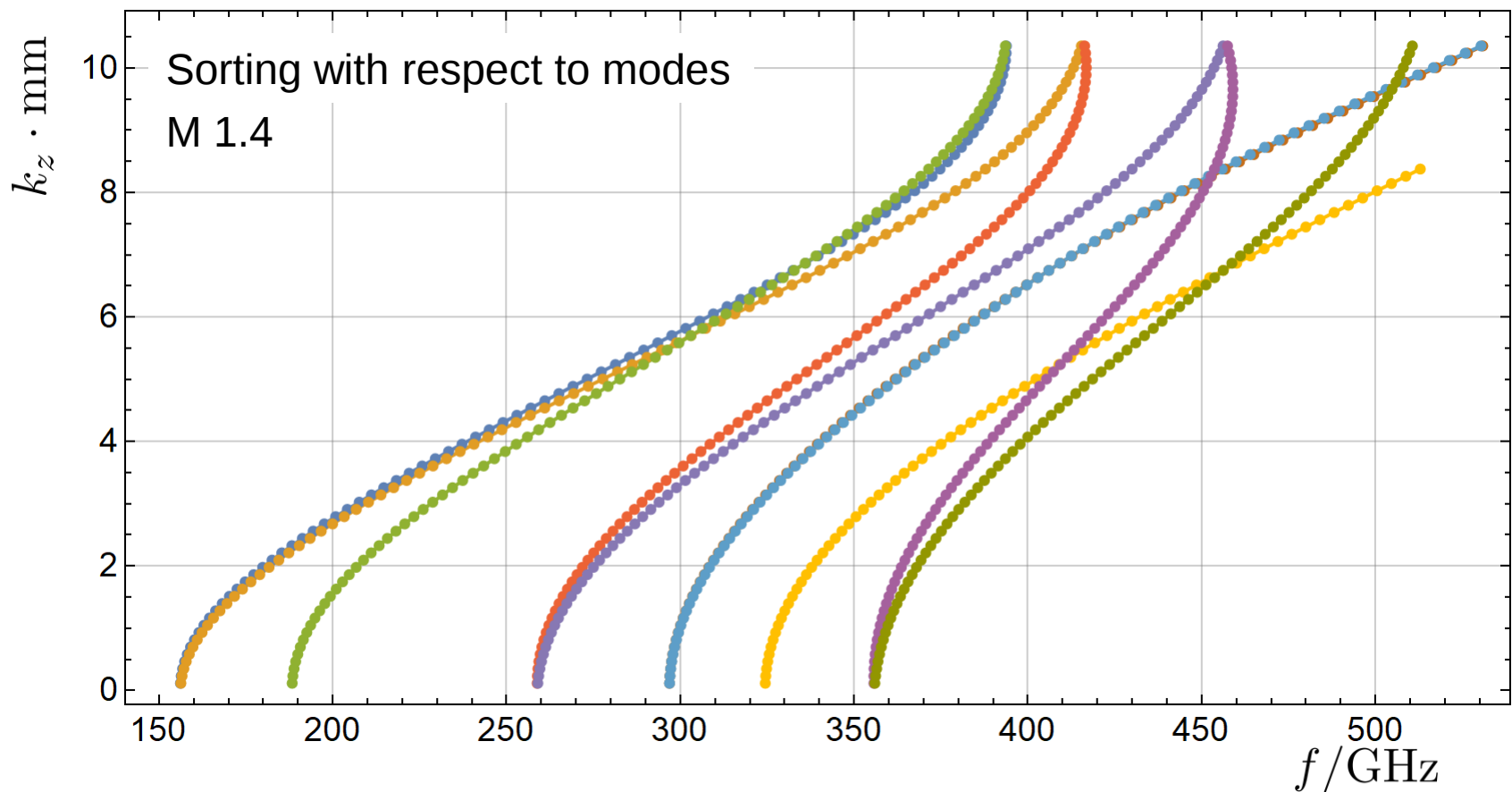
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



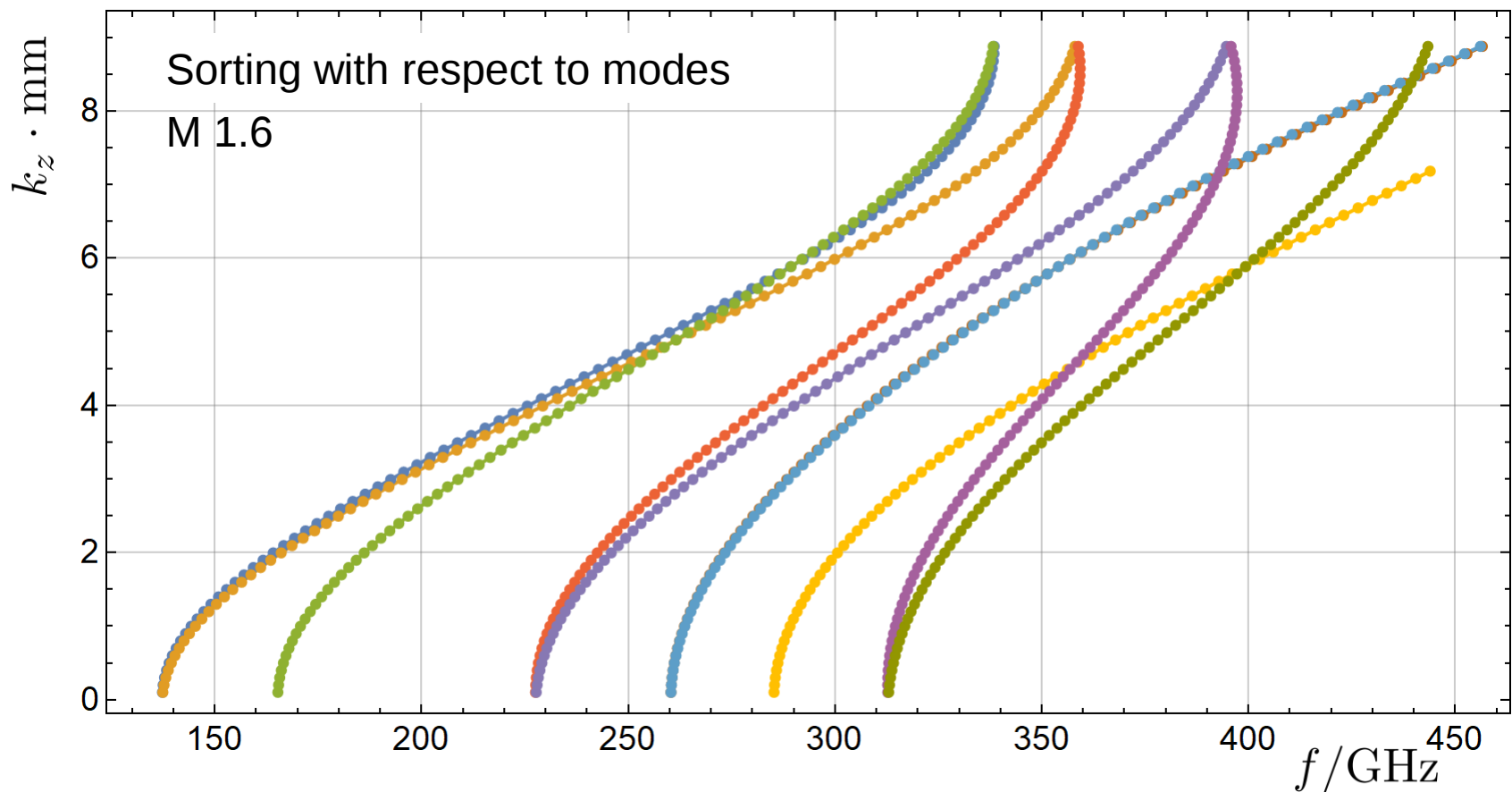
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



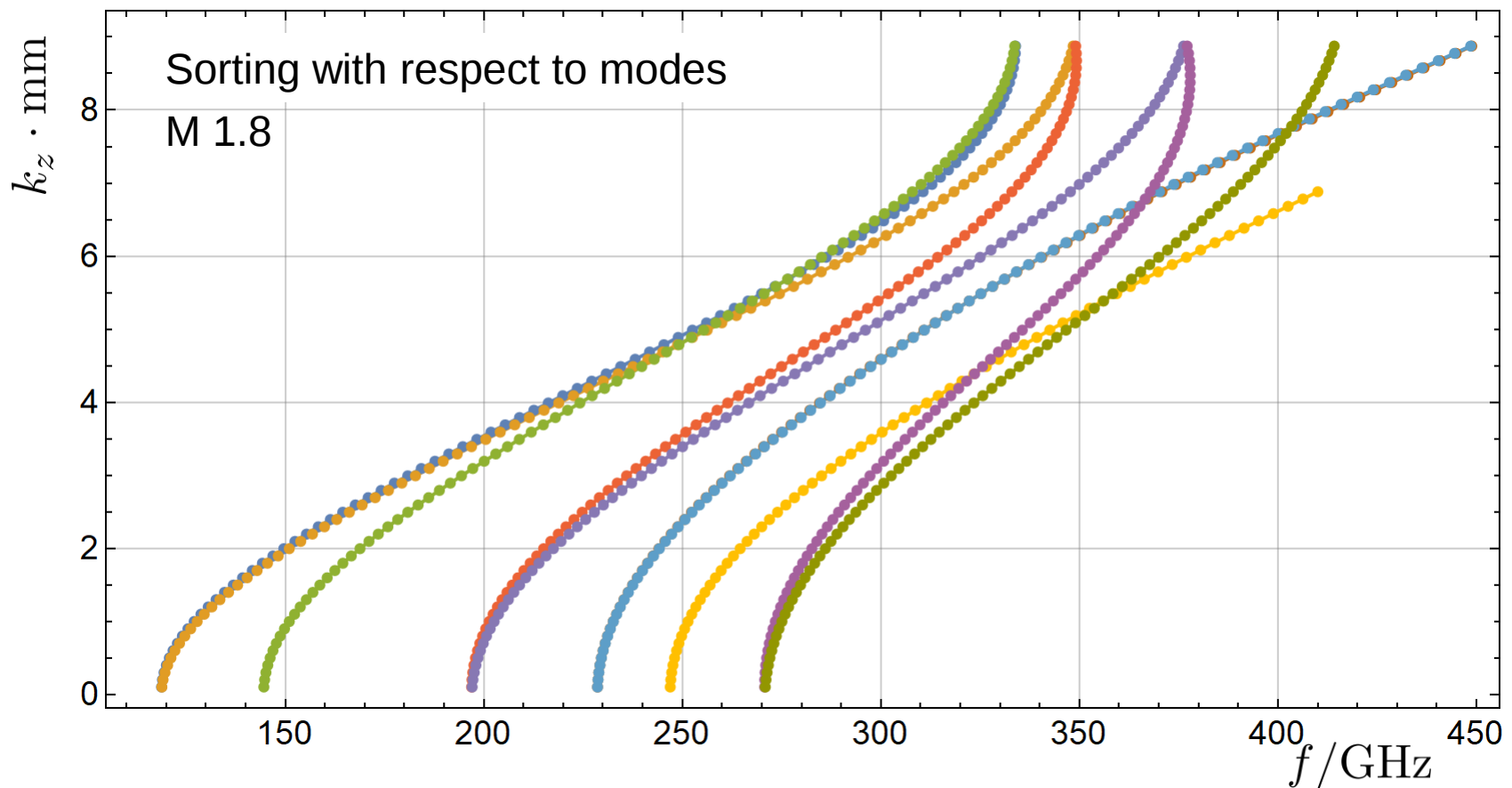
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



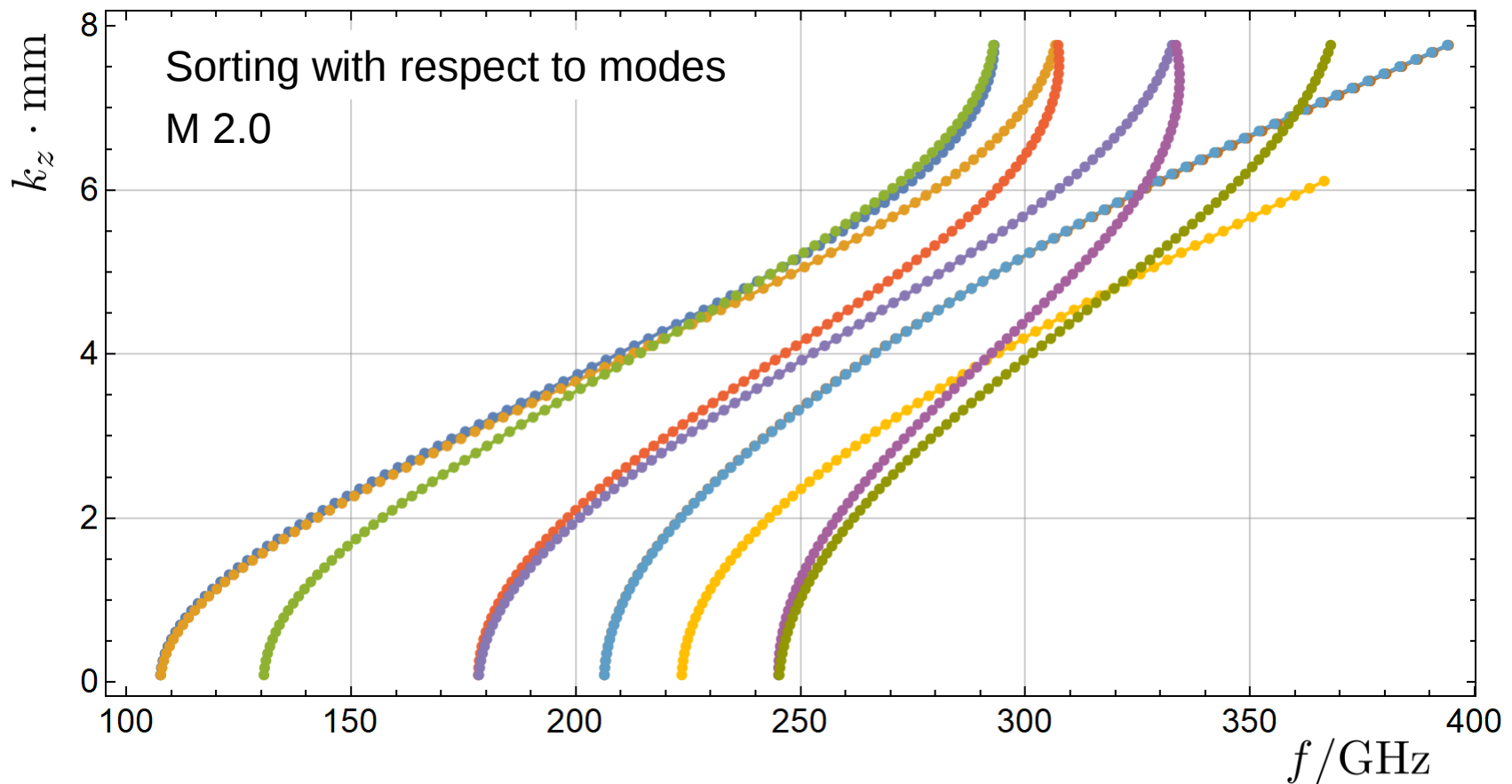
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



Numerical Results

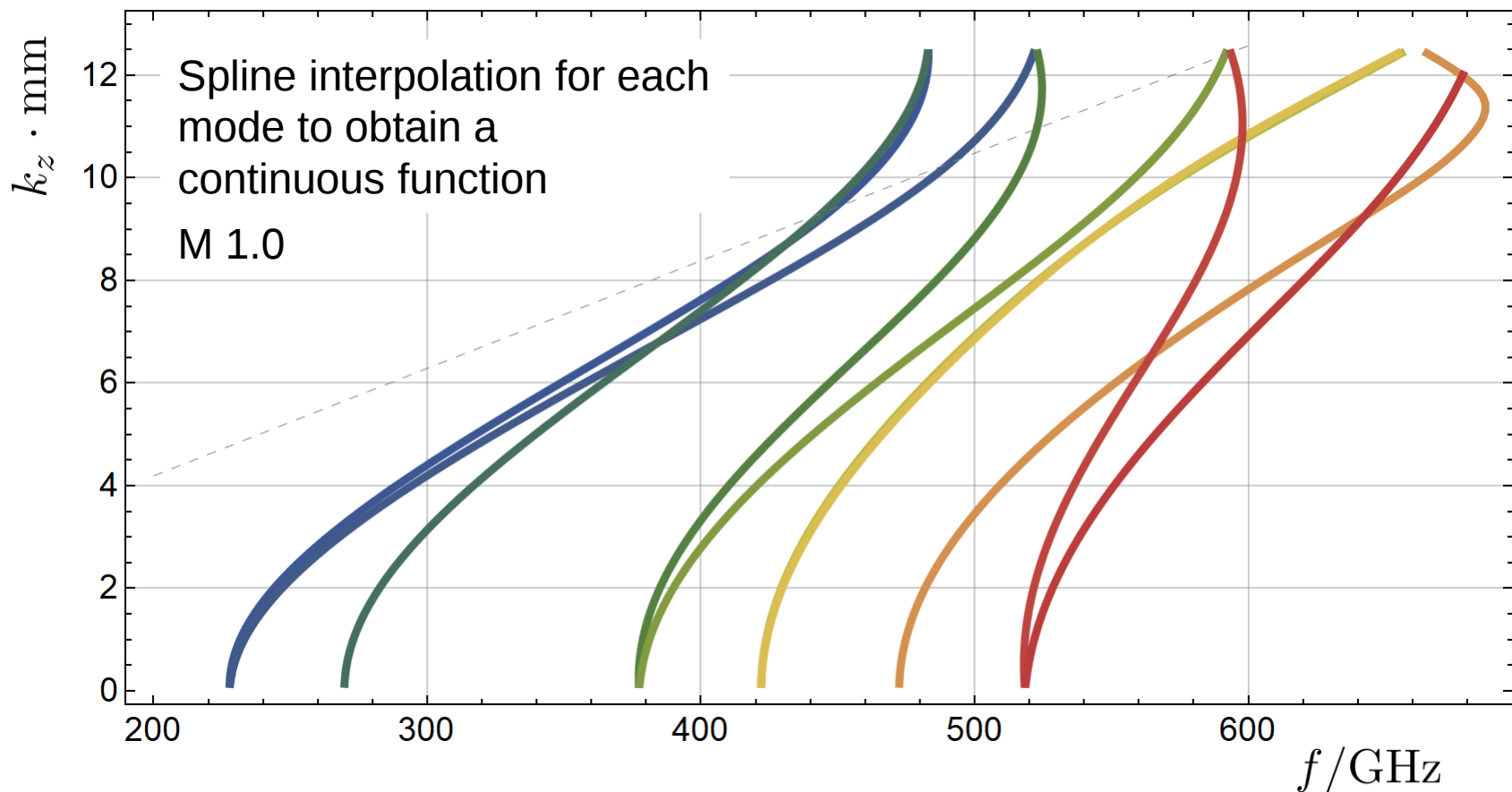
■ Dispersion Diagram (ISO metric screw thread)



- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

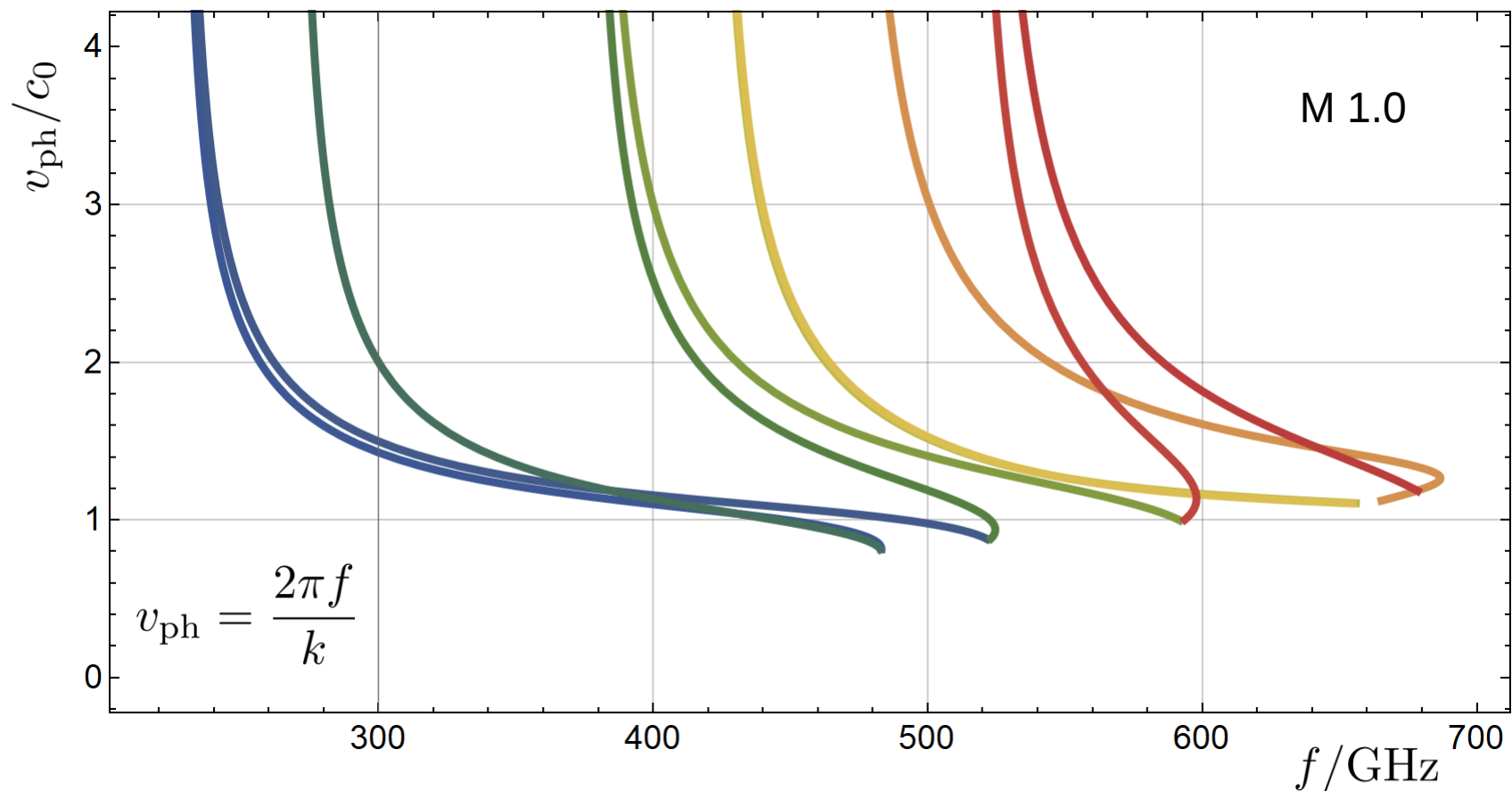
Numerical Results

■ Dispersion Diagram (ISO metric screw thread)



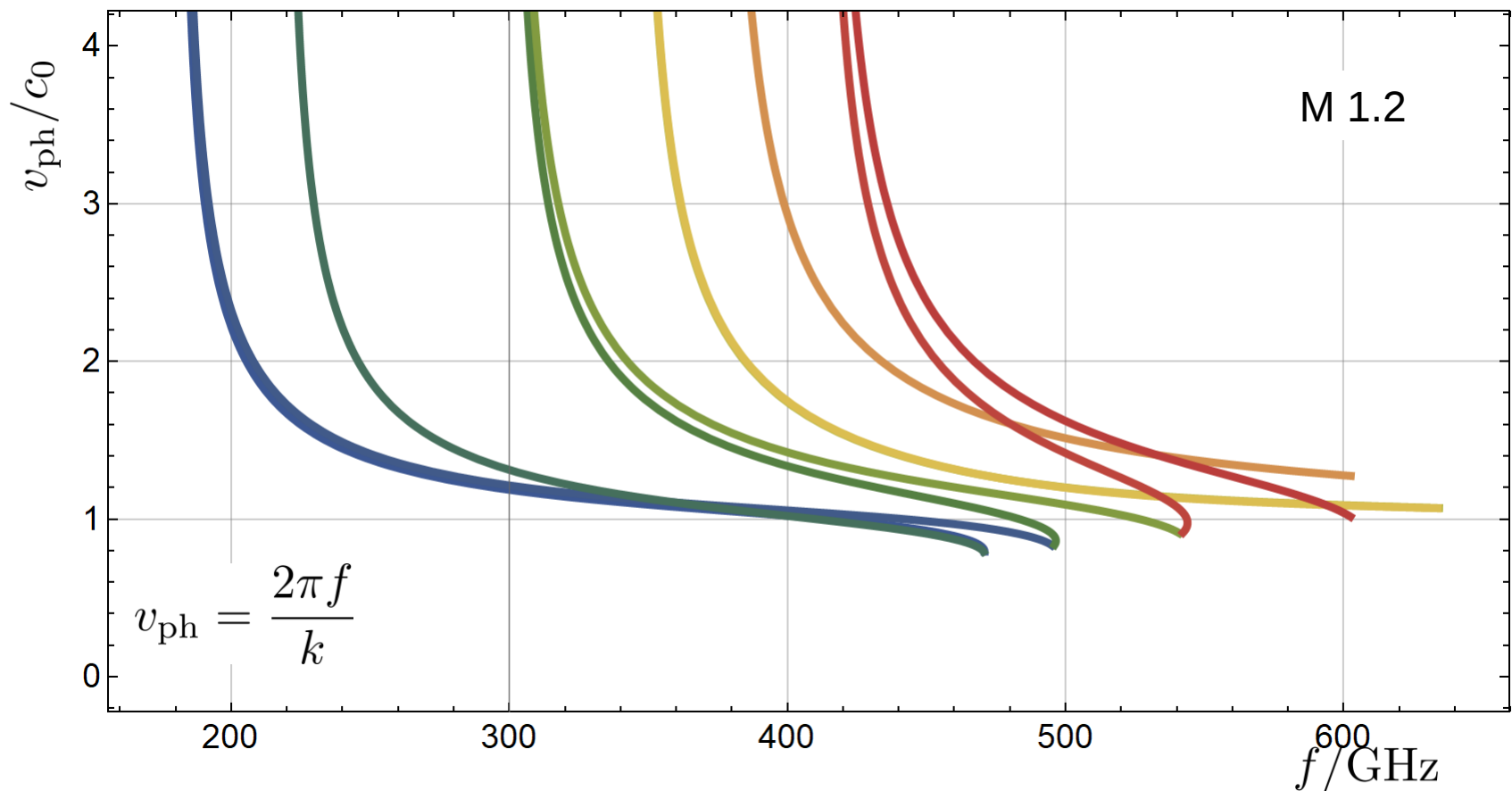
Numerical Results

■ Phase Velocity (ISO metric screw thread)



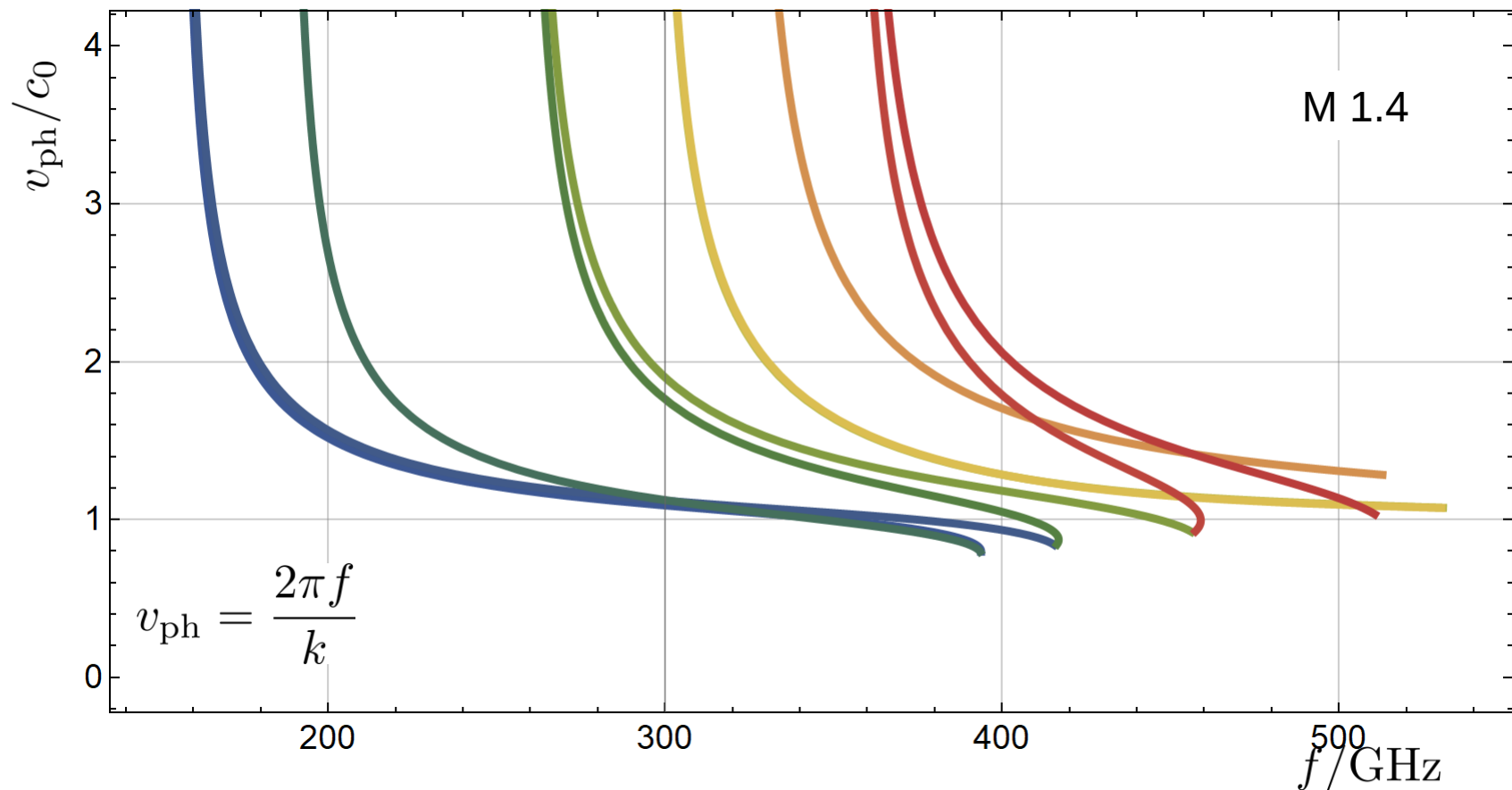
Numerical Results

■ Phase Velocity (ISO metric screw thread)



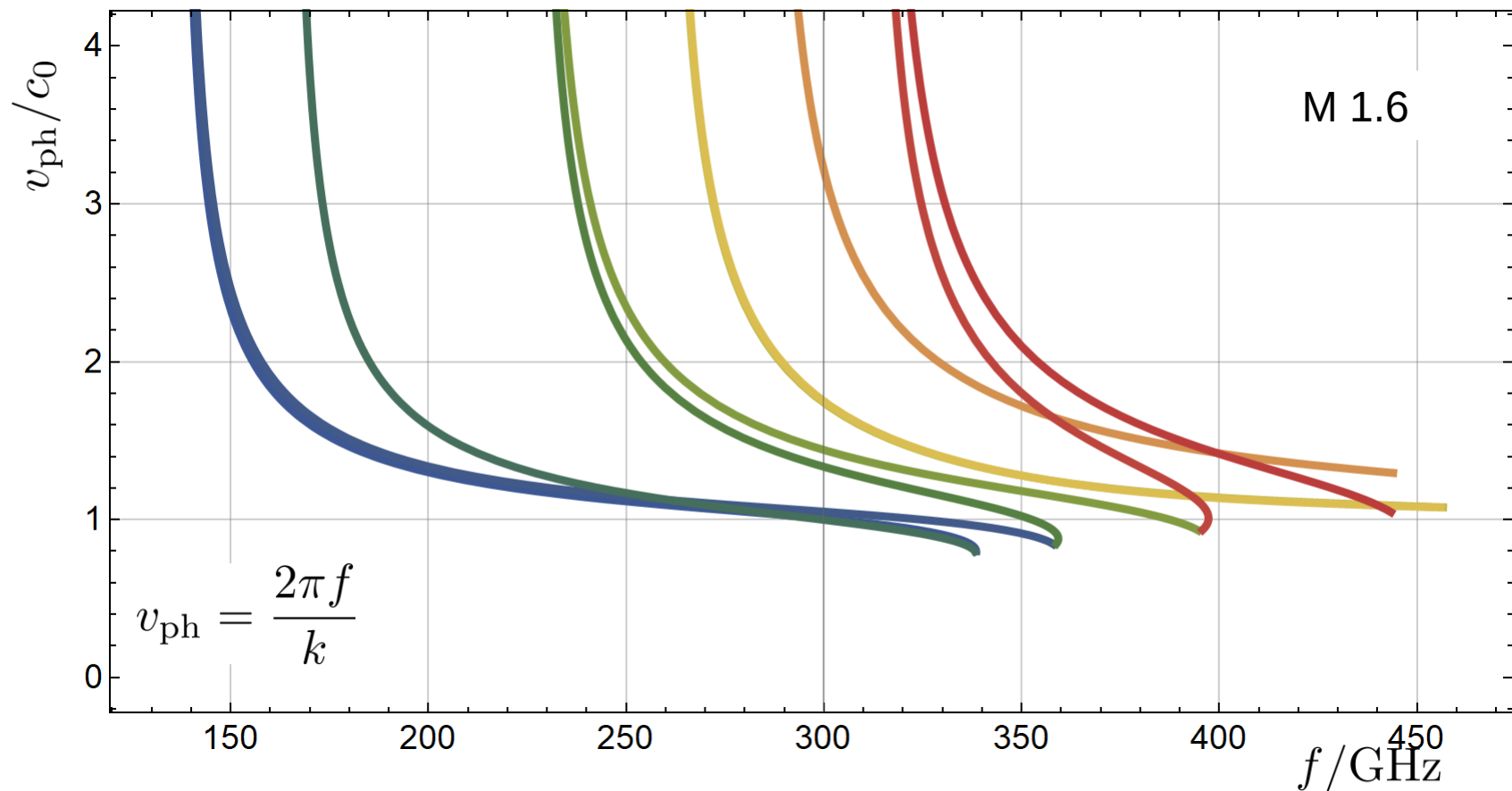
Numerical Results

■ Phase Velocity (ISO metric screw thread)



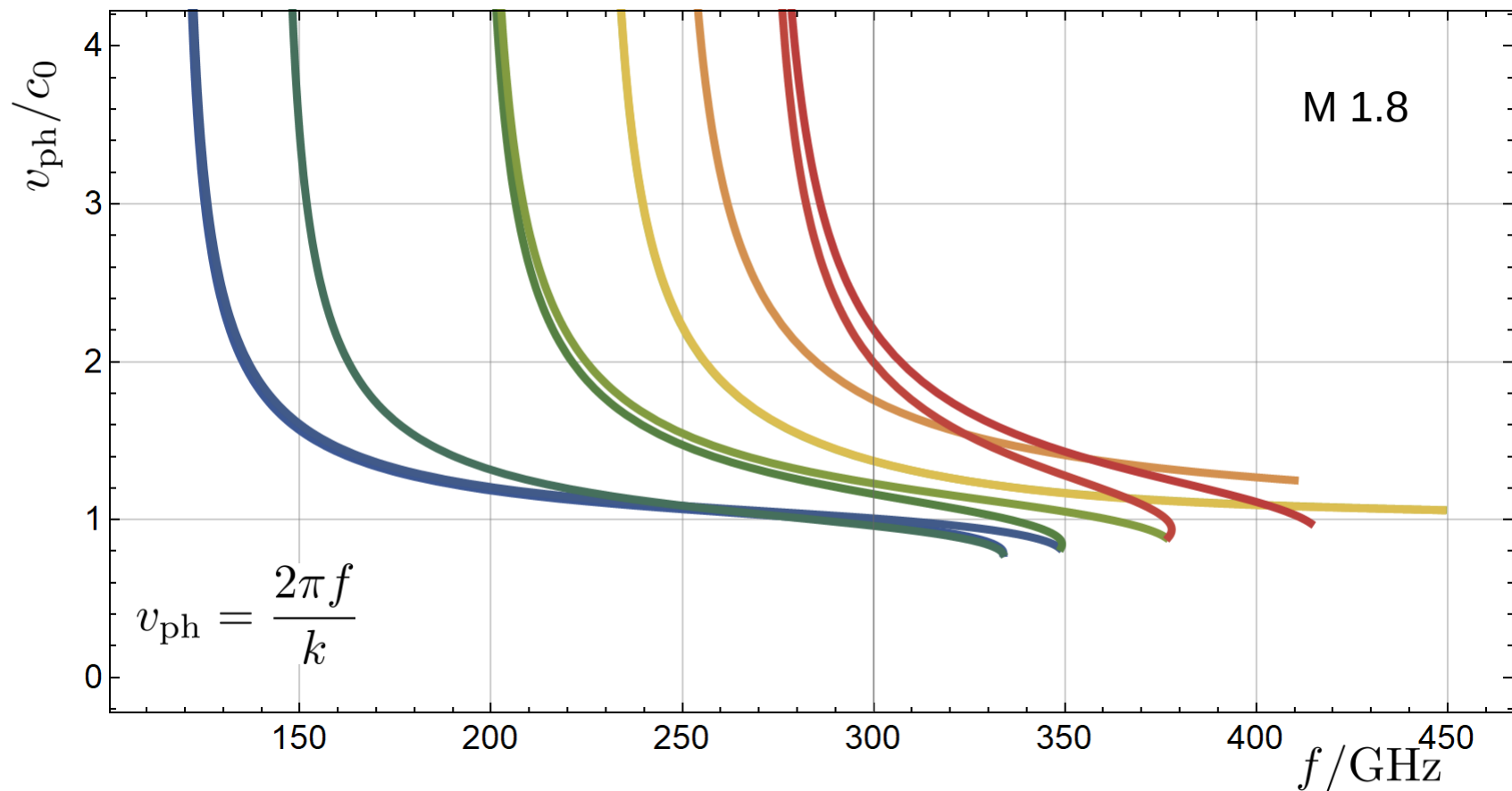
Numerical Results

■ Phase Velocity (ISO metric screw thread)



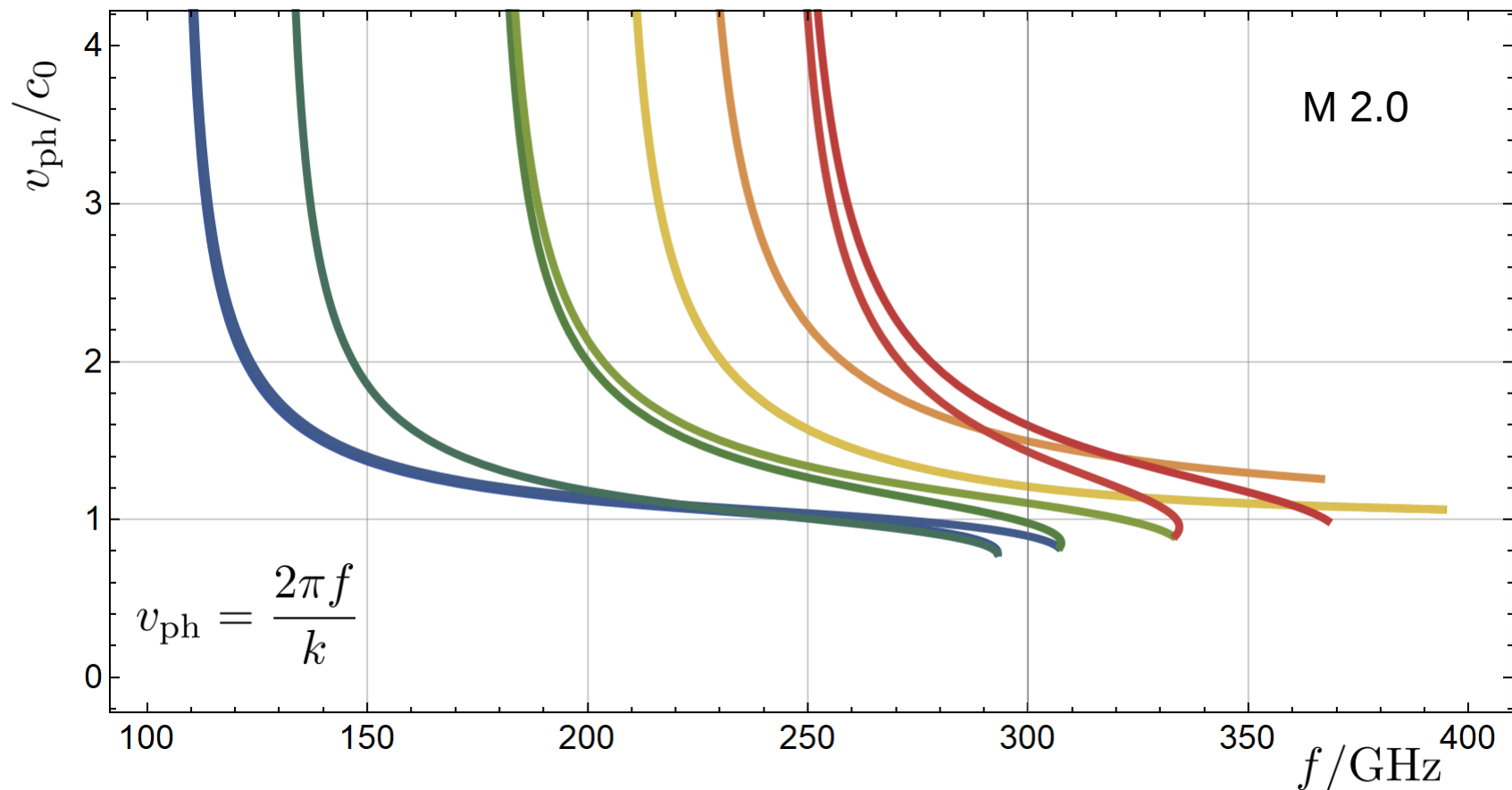
Numerical Results

■ Phase Velocity (ISO metric screw thread)



Numerical Results

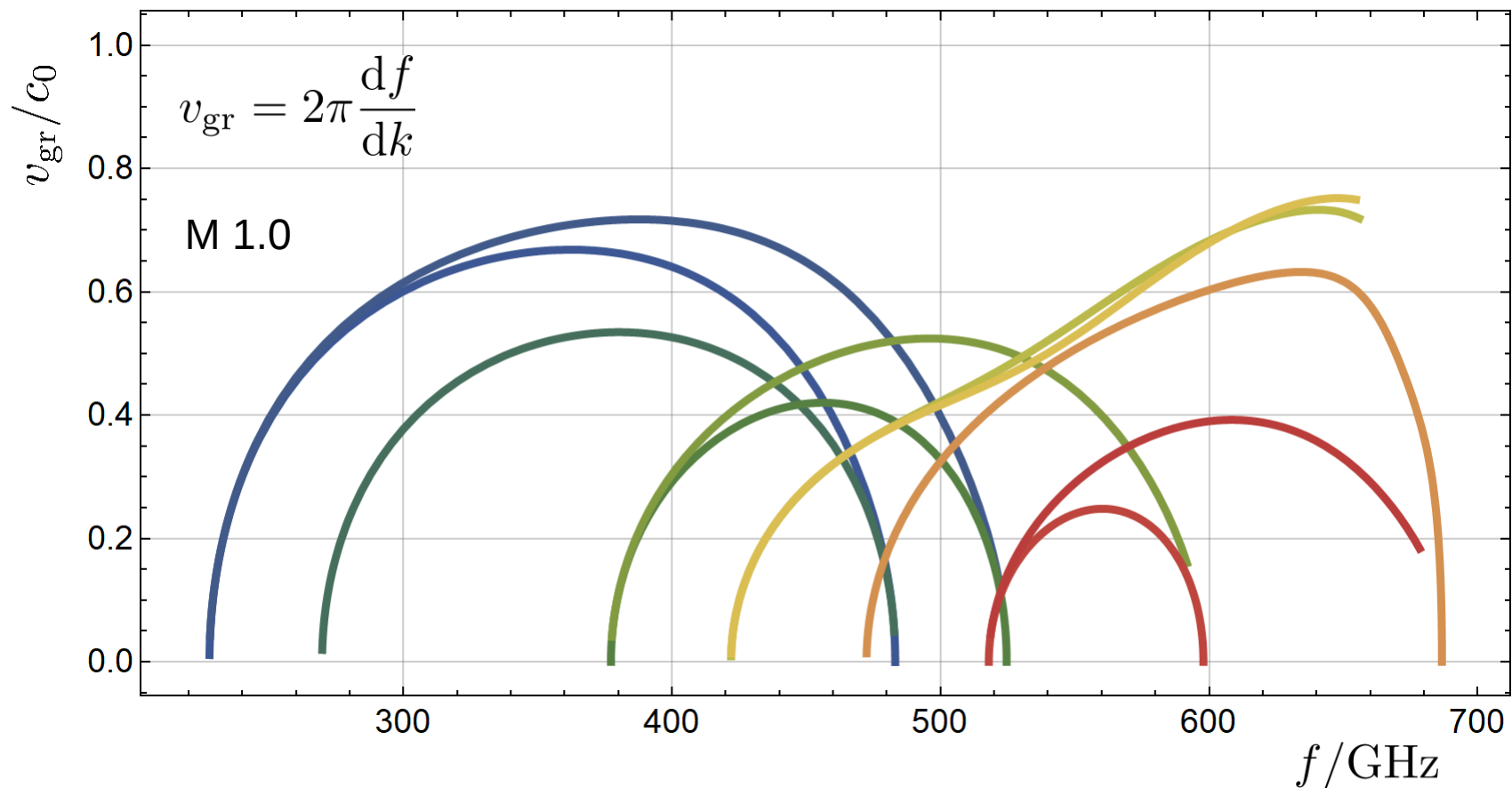
■ Phase Velocity (ISO metric screw thread)



- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

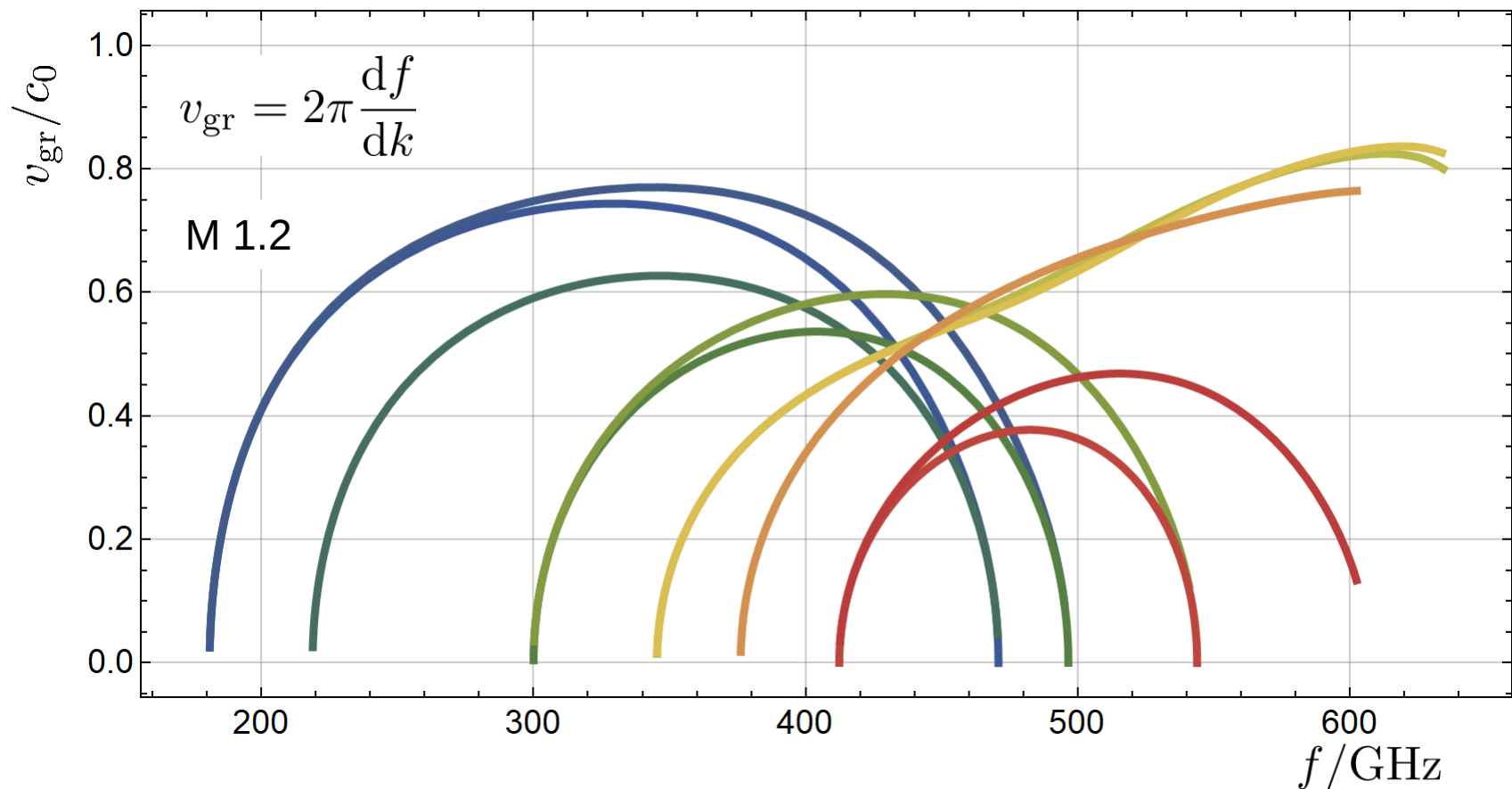
Numerical Results

■ Group Velocity (ISO metric screw thread)



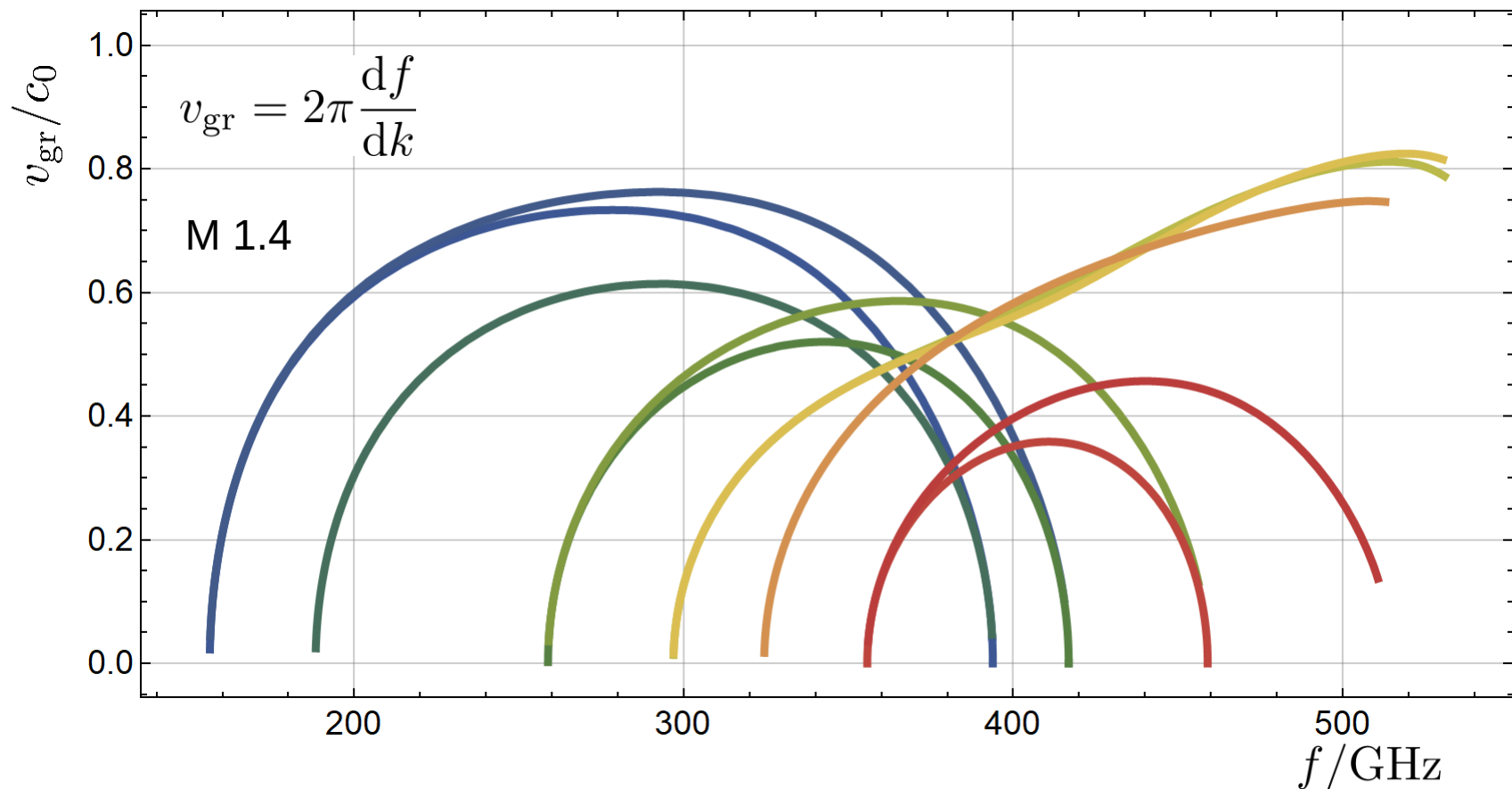
Numerical Results

- Group Velocity (ISO metric screw thread)



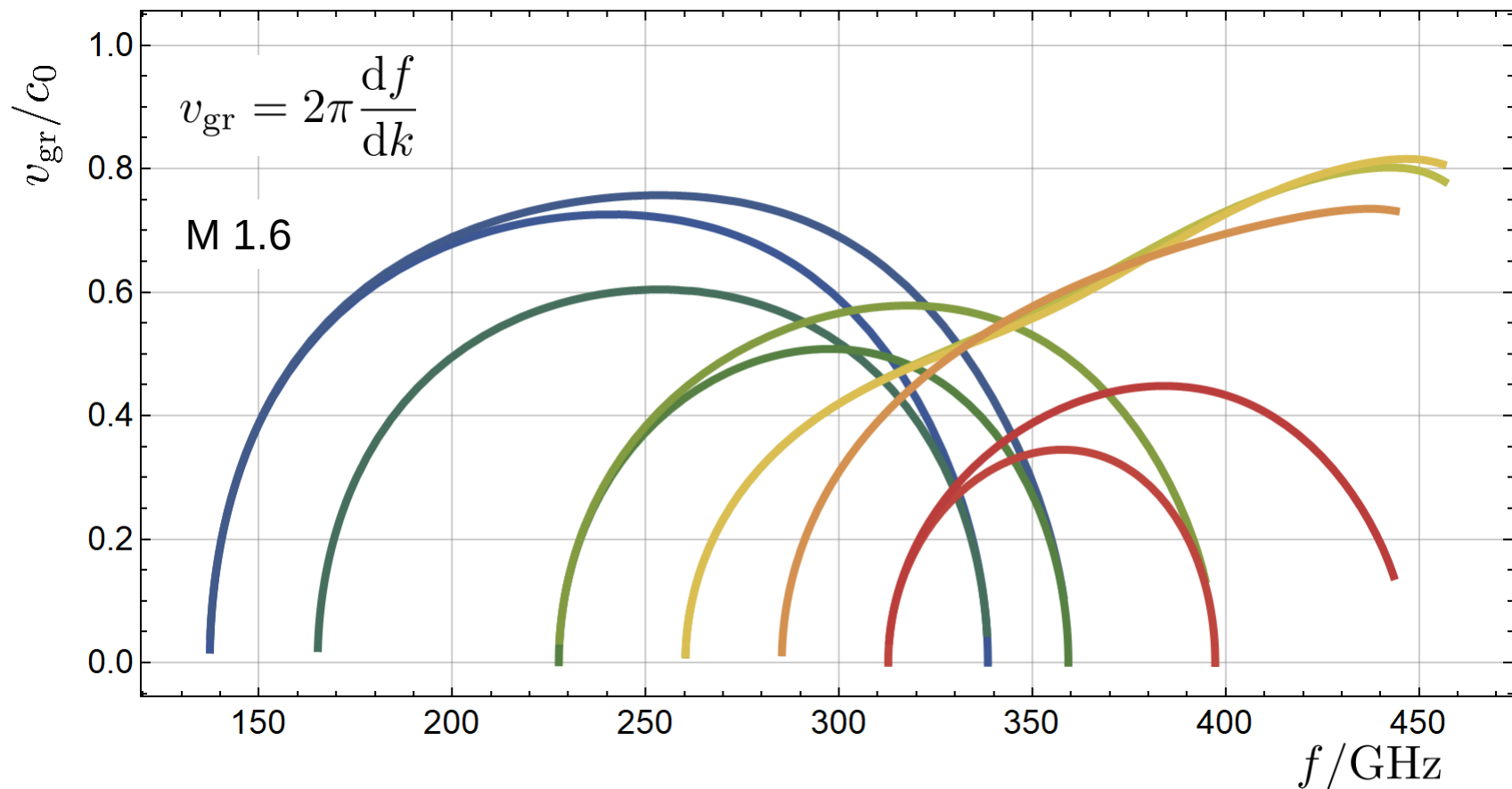
Numerical Results

■ Group Velocity (ISO metric screw thread)



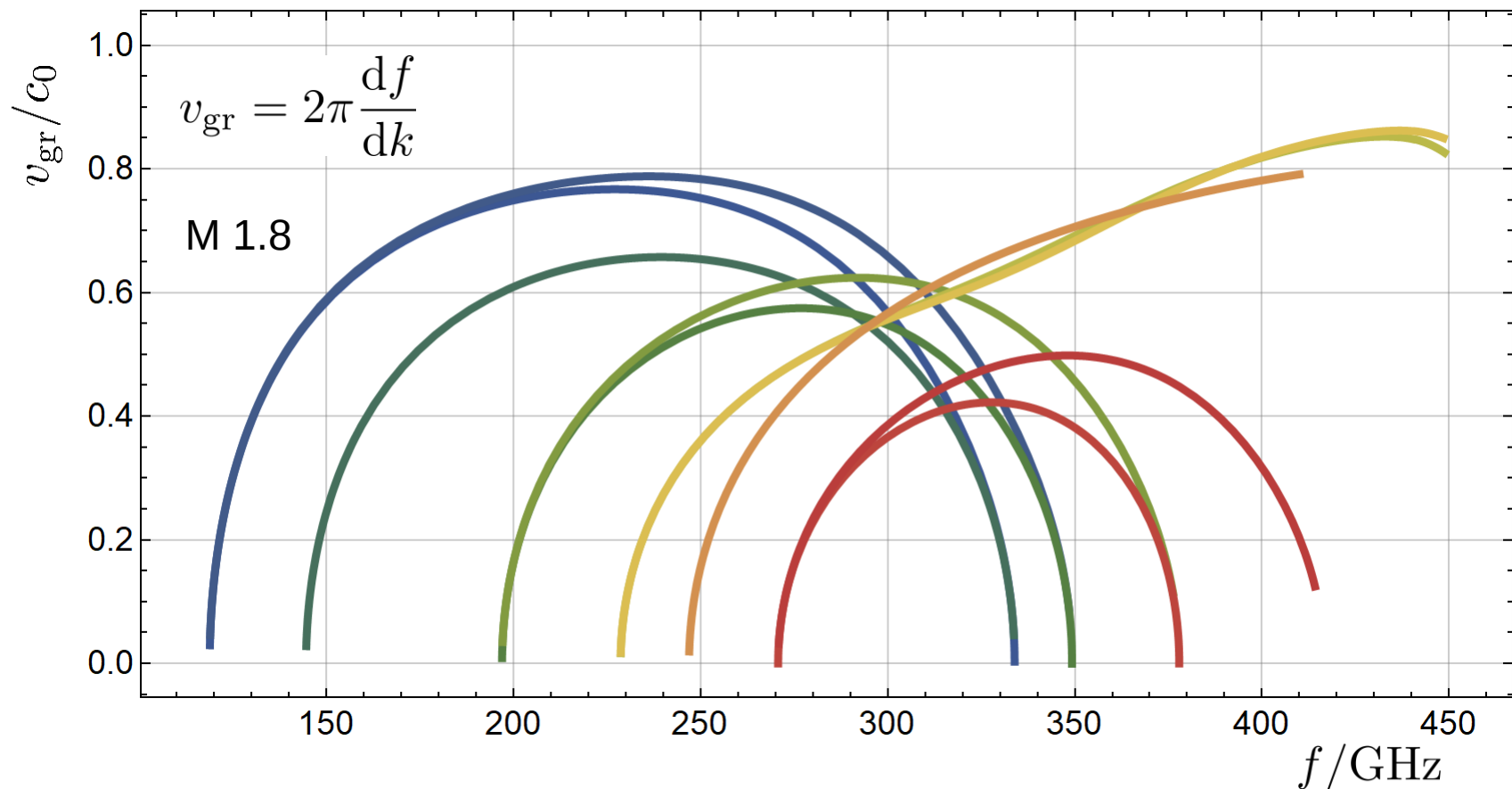
Numerical Results

■ Group Velocity (ISO metric screw thread)



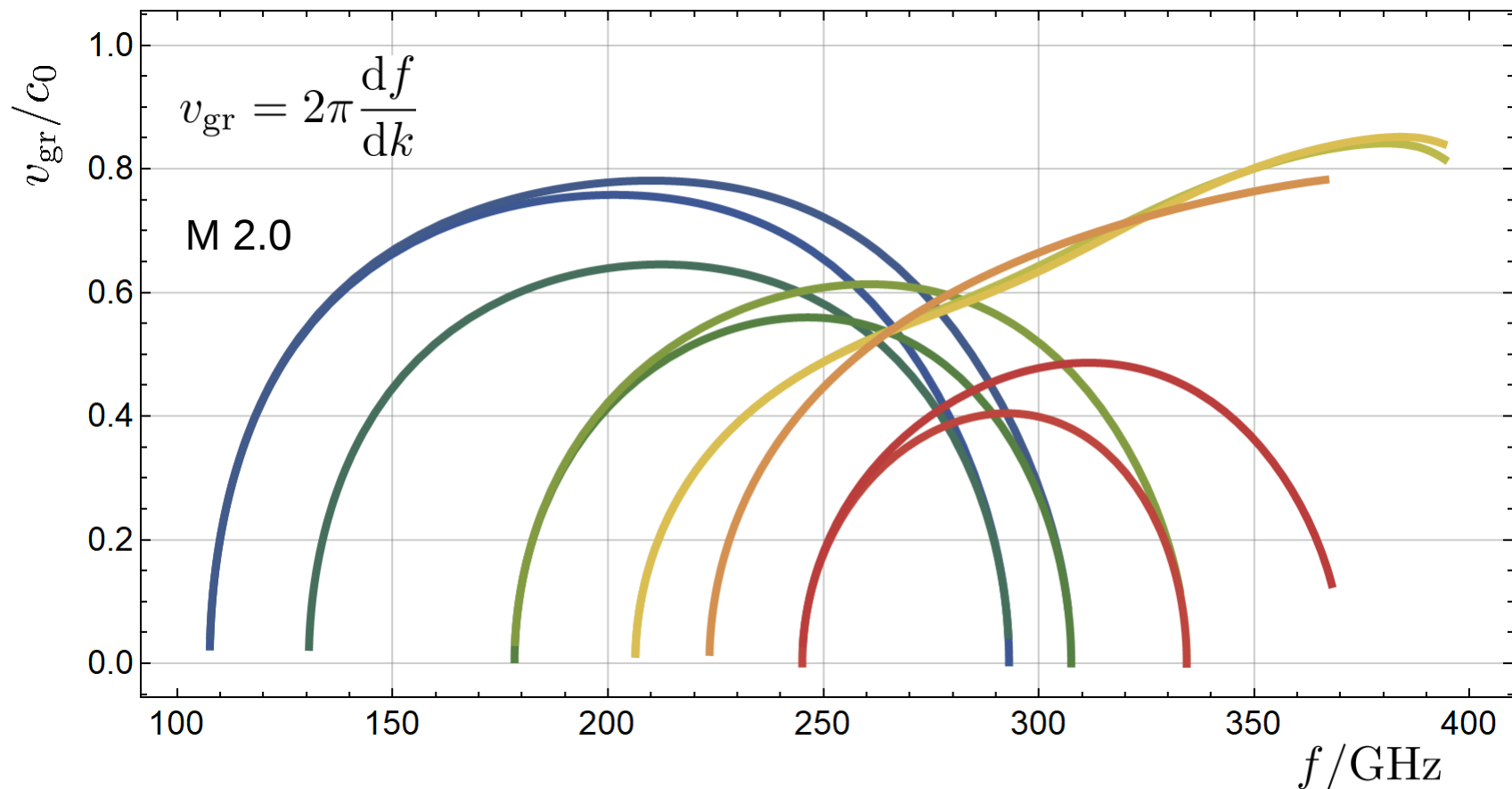
Numerical Results

■ Group Velocity (ISO metric screw thread)



Numerical Results

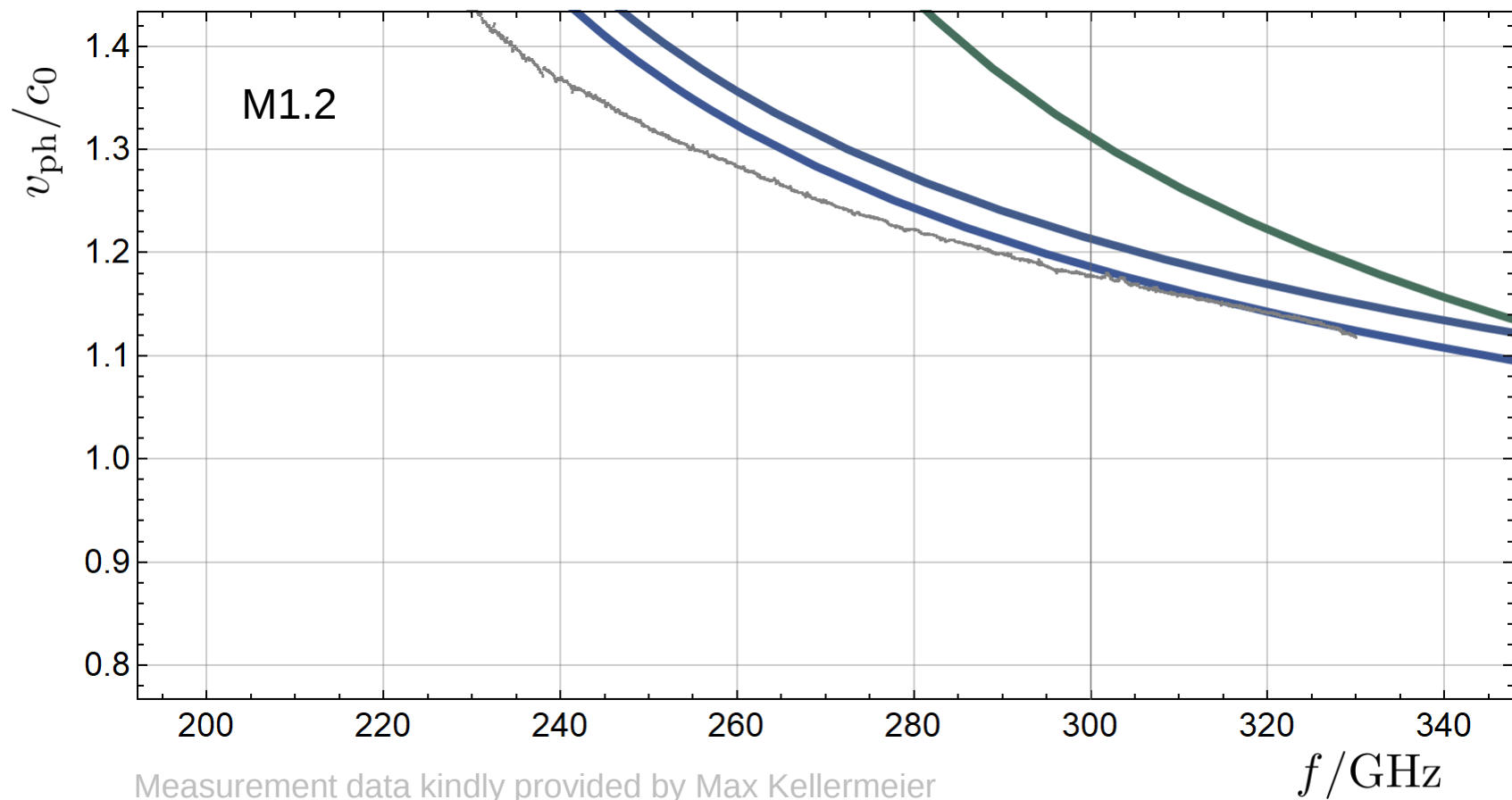
- Group Velocity (ISO metric screw thread)



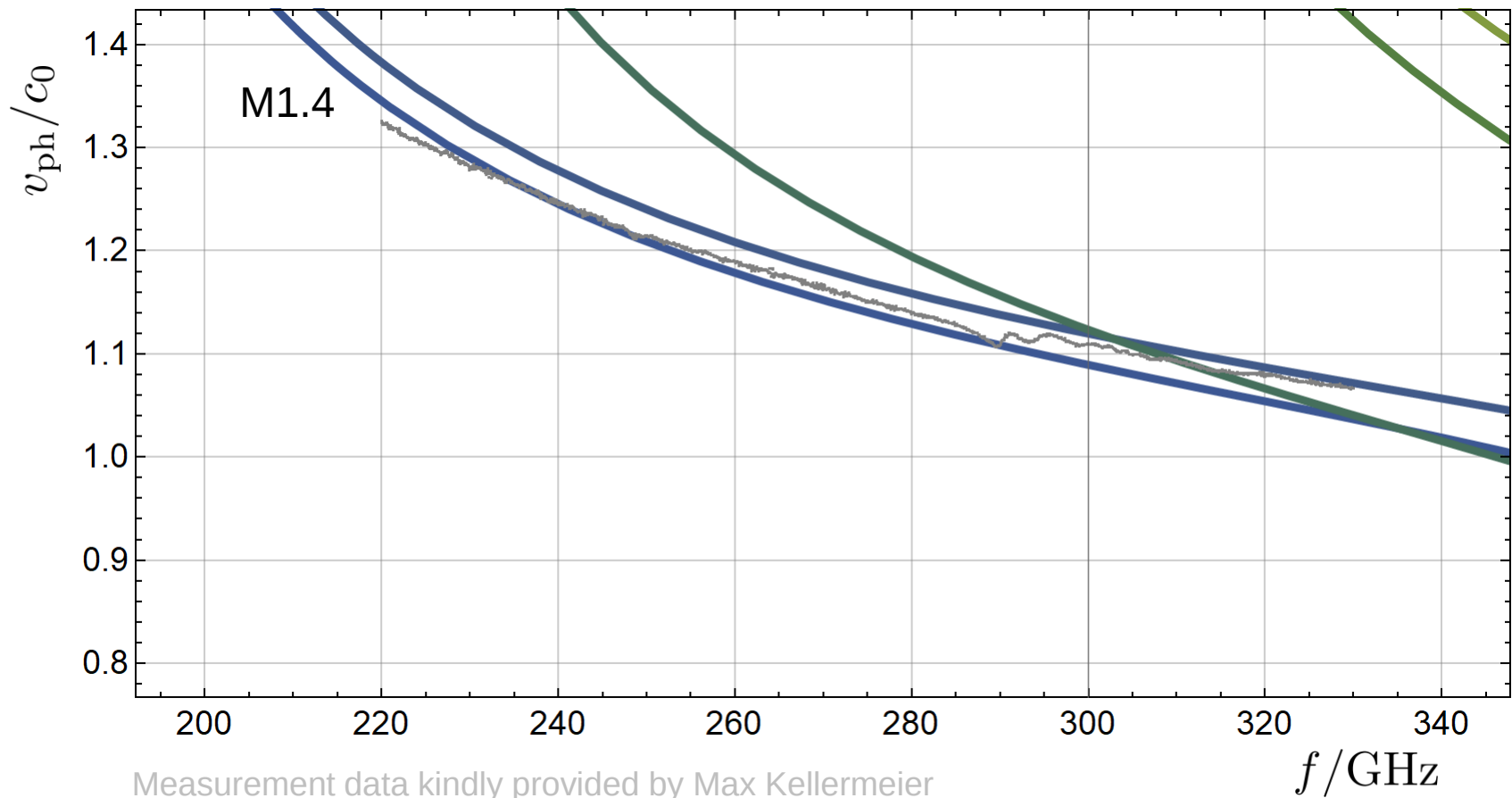
- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

Numerical Results

■ Phase Velocity: Simulation vs. Measurement

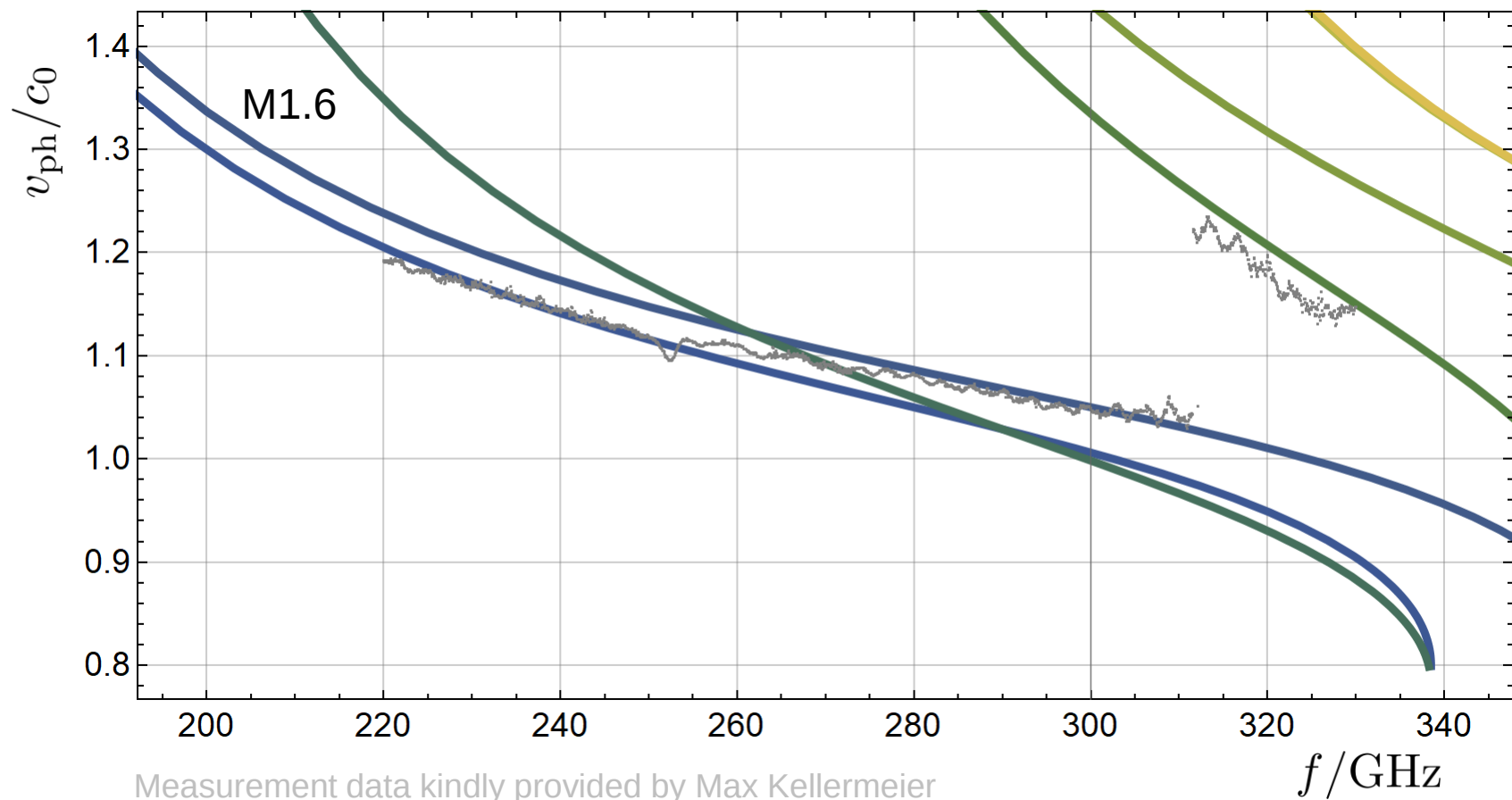


■ Phase Velocity: Simulation vs. Measurement



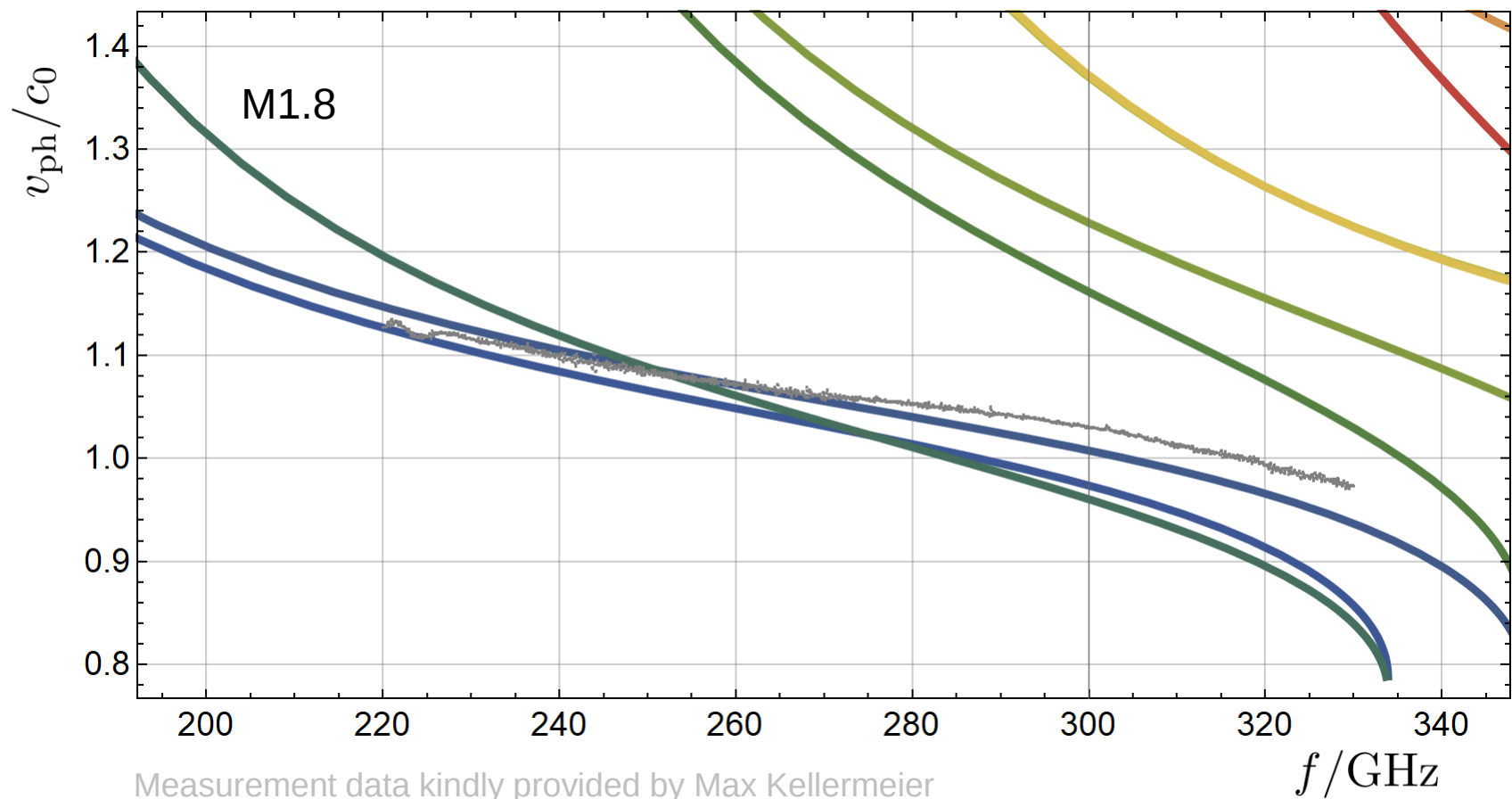
Numerical Results

■ Phase Velocity: Simulation vs. Measurement



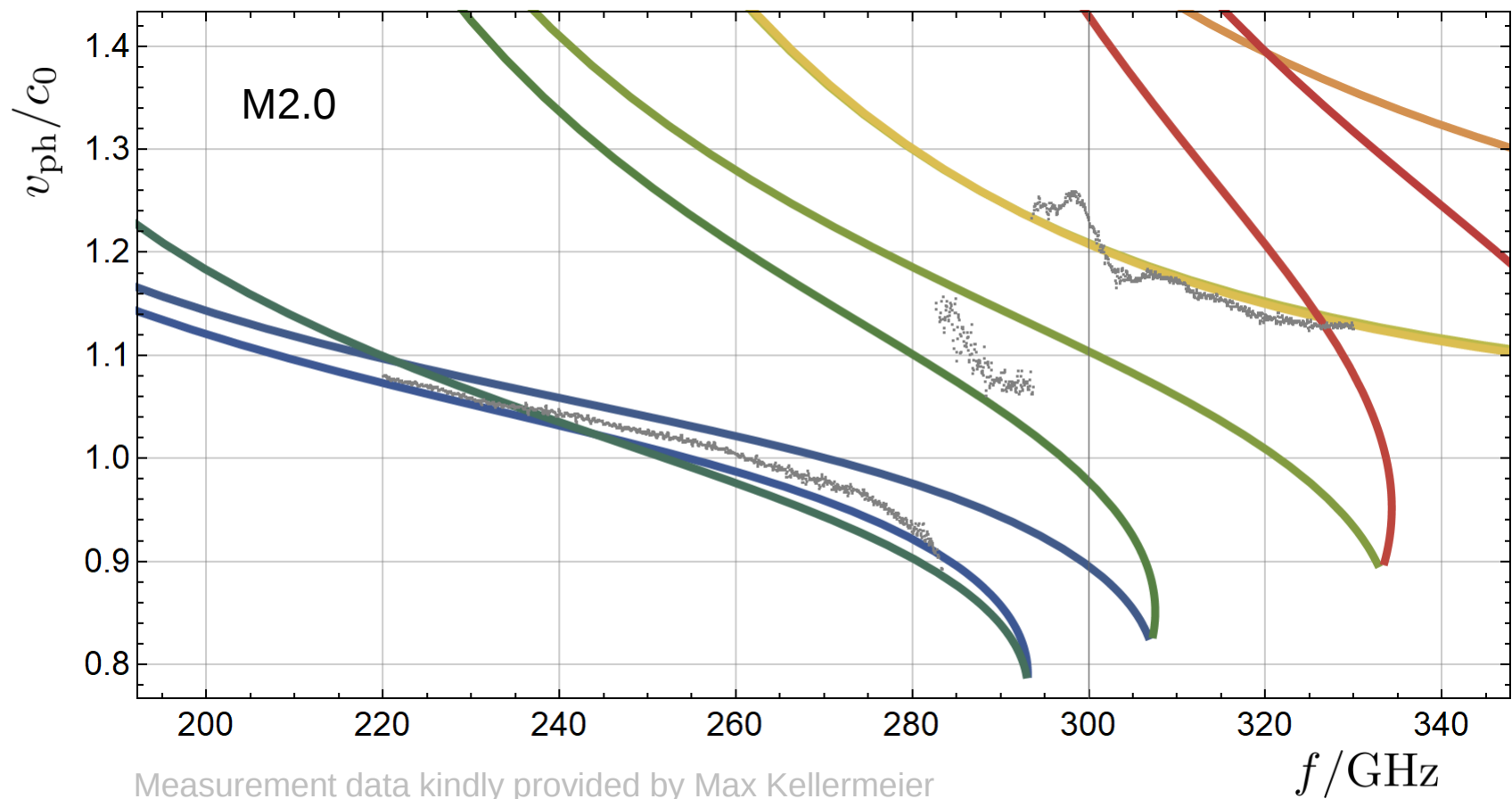
Numerical Results

■ Phase Velocity: Simulation vs. Measurement



Numerical Results

■ Phase Velocity: Simulation vs. Measurement



- Motivation
- Numerical Modeling
 - Dispersion Diagram
 - Ordering with respect to Frequency or Modes
- Numerical Results
 - Dispersion Diagram for M1.0 to M2.0 in Steps of 0.2
 - Postprocessing
 - Phase Velocity
 - Group Velocity
 - Comparison to Measurements
- Summary and Outlook

▪ Summary

- Determination of the dispersion diagram using a 3D eigenvalue solver with phase-shifted boundary conditions
- Sorting of the results in terms of modes instead of the natural frequency
- Postprocessing of the raw data to obtain phase and group velocities

▪ Outlook

- Perform geometry variations to better understand the differences to the measurements
- Waveguide mode excitation based on a particle beam

